

# Realization of thermal inflation in SUSY discrete flavour symmetry model

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in collaboration with Y.Shimizu, T.Shimomura and Y.Nakagawa

# Introduction

## ◎ Discrete flavour symmetry

[ex: Ishimori et.al ('10)]

- suggested from neutrino experimental data,
- based on the non-Abelian discrete groups, (ex:  $A_4, S_4, \Delta(54) \dots$ )
- elegantly derive the flavour structures of elementally particles,
- naturally explain the mass spectrum...

## ◎ Flavon

[ex: Altarelli et.al ('05)]

- Gauge singlet scalar fields.
- VEVs of flavons derive the flavour structures via "*vacuum alignment*"
- generate the masses of leptons (ex: Heavy RH v's)
- Controlled by flavour symm. &  $Z_n$  symm. &  $U(1)_R$  symm.

# Problems of disc. flavour symm.

◎ However, SUSY discrete flavour symmetry model has problems...

- Domain wall problem
- Origin of vacuum structure of flavon
- Deviation from Tri-bimaximal mixing
  - ⋮
- Existence of pseudo moduli of flavon

Our focus!

# Pseudo moduli flavon

◎F-flat direction among the flavon fields

Expected to spontaneously breaks the flavour symmetry

$$V(|u|) = V_0 - \underline{\tilde{m}_u^2 |u|^2} + \Delta V_{\nu_R} + \Delta V_{\tilde{\nu}_R} \quad (W \ni y_R u \nu_R^c \nu_R^c)$$

Soft SUSY breaking mass

1-loop effective  
potential  
[ex:Bando et.al ('93)]

$$\left( \begin{array}{l} \Delta V_{\nu_R} = - \sum_{i=1}^3 \frac{|y_{Ri}|^4 |u|^4}{32 \pi^2} \left[ \ln \left( \frac{|y_{Ri}|^2 |u|^2}{\tilde{m}_u^2} \right) - \frac{3}{2} \right] \\ \Delta V_{\tilde{\nu}_R} = \sum_{i=1}^3 \frac{(\tilde{m}_{\nu_R i}^2 + |y_{Ri}|^2 |u|^2)^2}{32 \pi^2} \left[ \ln \left( \frac{\tilde{m}_{\nu_R i}^2 + |y_{Ri}|^2 |u|^2}{\tilde{m}_u^2} \right) - \frac{3}{2} \right] \end{array} \right)$$

# Pseudo moduli flavon

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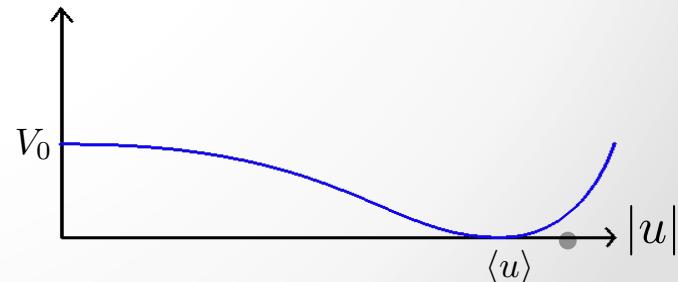
$$V(|u|) = V_0 - \tilde{m}_u^2 |u|^2 + \Delta V_{\nu_R} + \Delta V_{\tilde{\nu}_R} \quad (W \ni y_R u \nu_R^c \nu_R^c)$$

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$$\langle u \rangle \simeq \frac{\tilde{m}_u}{\sqrt{|y_R|^2}} \exp \left( \frac{8\pi^2 \tilde{m}_u^2}{3 |y_R|^2 \tilde{m}_{\nu_R}^2} \right)$$

**Strongly depend on  
Soft SUSY breaking mass  
[ H.N & Y.Shimizu ('12)]**

$$V_0 = \frac{3 |y_R|^2}{16 \pi^2} \tilde{m}_{\nu_R}^2 \langle u \rangle^2$$



# Thermal history of pseudo moduli flavon

- Once, we consider the thermal history of flavon...

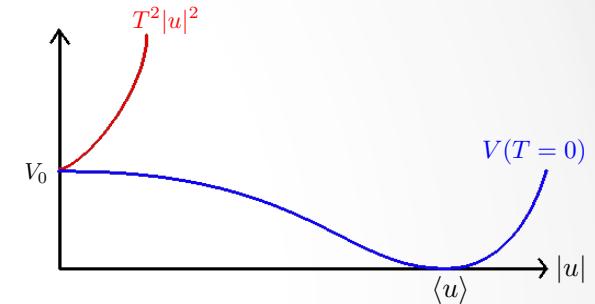
$$V(|u|) = V_0 - \tilde{m}_u^2 |u|^2 + \Delta V_{\nu_R} + \Delta V_{\tilde{\nu}_R} + c T^2 |u|^2$$

◎ Thermal evolution of flavon

$T$



$T \gg \tilde{m}_u$  :  $u$  trapped at origin by thermal potential



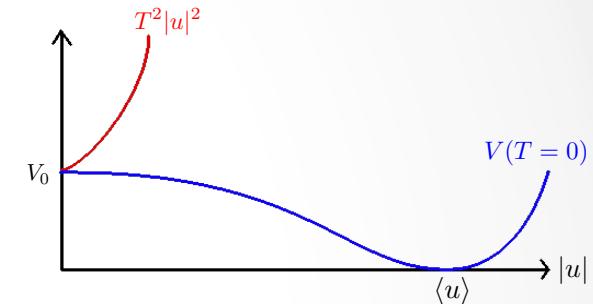
$T < \tilde{m}_u$  :  $u$  rolls down to the minimum  
→  $u$  obtain non-vanishing VEV

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$$V(|u|) = V_0 - \tilde{m}_u^2 |u|^2 + \Delta V_{\nu_R} + \Delta V_{\tilde{\nu}_R} + c T^2 |u|^2$$

◎ Thermal evolution of flavon



T

$T \gg \tilde{m}_u$  : u trapped at origin  
by thermal potential

$T < V_0^{1/4}$  : Start to dominate the energy of universe

$T < \tilde{m}_u$  : u rolls down to the minimum  
→ u obtain non-vanishing VEV

$T = T_R^{(sec)}$  : Energy transfer from u into SM

Must above few MeV

Realize in the flavour symm. models??

# Decay rate of flavon

[ H.N & Y.Shimizu ('12)]

◎Interaction lagrangian ( $W \ni y_R u \nu_R^c \nu_R^c$ )

$$\mathcal{L}_{int} \ni \frac{y_R}{2\sqrt{2}} \delta u \nu_R^c \nu_R^c + h.c. + \frac{\delta u}{\sqrt{2} \langle u \rangle} (\partial_\mu a)^2$$

$$u \equiv \left( \langle u \rangle + \frac{\delta u}{\sqrt{2}} \right) \exp \left( i \frac{a}{\sqrt{2}v} \right)$$

◎Decay rate of pseudo moduli flavon

$$\Gamma(u \rightarrow 2a) \simeq \frac{1}{64\pi} \frac{m_u^3}{\langle u \rangle^2} \quad \leftarrow \quad \text{Dominate decays of } u$$

$$\text{Br}(u \rightarrow 2a) \simeq 1$$

$$\Gamma(u \rightarrow 2\nu) \simeq \frac{3}{16\pi} \left( \frac{m_\nu}{\langle u \rangle} \right)^2 m_u$$

$$\begin{pmatrix} m_u^2 \simeq \frac{3|y_R|^2 \tilde{m}_{\nu_R}^2}{4\pi^2} \\ \underline{\underline{m_a \simeq 0}} \end{pmatrix}$$

◎Reheating temperature after u domination

$$T_R^{(sec)} \simeq 0.45 \sqrt{\Gamma(a \rightarrow \text{SM}) M_p}$$

$$T_R^{(sec)} \ll 1 \text{ MeV}$$

**Energy transfer from flavon  
does NOT complete  
before BBN!!**

# Possible solutions

[ H.N & Y.Shimizu ('12)]

## Problem

Energy transfer from u  
complete before BBN?

(Realize  $\text{Br}(u \rightarrow 2a) \ll 1$  ??)

3) Explicit breaking term  
of disc. flav. symm.

$$\Delta\mathcal{L} = -\kappa (u + u^*)$$

+ Coupling with  
vector-like “quarks”

2) Introduce the coupling with  
vector-like “quarks”  $\Delta W = y_Q u Q \bar{Q}$

1) Light RH neutrino  $m_{\nu_R} \leq m_u/2$   
via higher-dim. operator

# Light RH neutrino

◎ Generate mass of RH $\nu$  by suppressed interaction [ H.N et. al ('12)]

$$W \ni y_R \frac{u^2}{\Lambda} \nu_R^c \nu_R^c \quad \Lambda : \mathcal{O}(M_p)$$

$$m_{\nu_R} \simeq \frac{|y_R| \langle u \rangle^2}{\Lambda}$$

Allow  $u \rightarrow \nu_R \nu_R$  on-shell

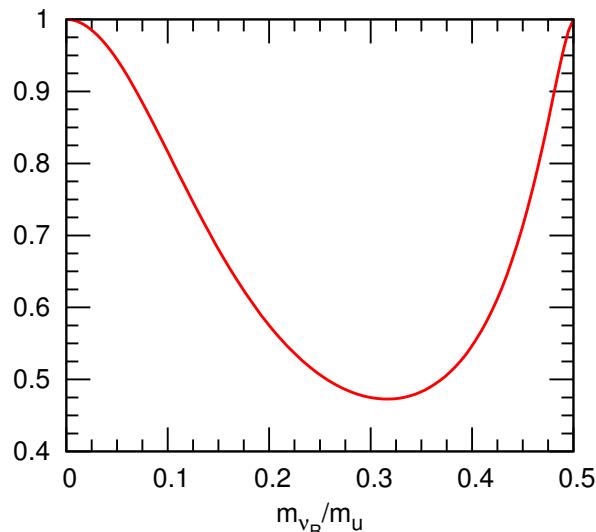
cf. usual charge assignment

$$W \ni y_R u \nu_R^c \nu_R^c$$

$$m_{\nu_R} \simeq |y_R| \langle u \rangle$$

$$\Rightarrow \mathcal{O}(10^{13} \text{ GeV})$$

◎ Branching ratio of decays of  $u$



$$Br(u \rightarrow 2a) \simeq \frac{\Gamma(u \rightarrow 2a)}{\Gamma(u \rightarrow 2a) + \Gamma(u \rightarrow 2\nu_R)} < 0.23 \text{ (BBN)}$$

[Cyburt et.al ('04)]

$$= \left( 1 + 24 \frac{m_{\nu_R}^2}{m_u^2} \beta_f^3 \right)^{-1} \leq 45 \%$$

$$\beta_f \equiv \sqrt{1 - 4m_{\nu_R}^2/m_u^2}$$

Not suppressed enough!

(※ But can reproduce the DayaBay result)

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[ H.N & Y.Shimizu ('12)]

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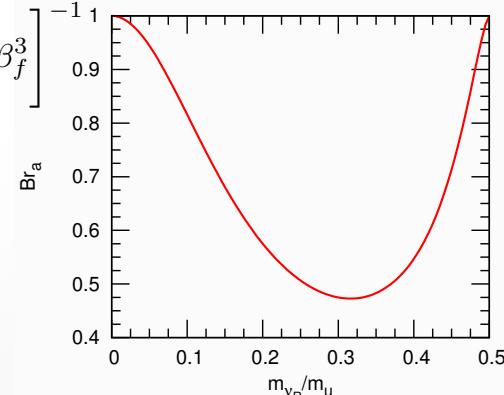
2) Introduce the coupling with vector-like "quarks"  $\Delta W = y_Q u Q \bar{Q}$

1) Light ~~RH neutrino~~  ~~$m_{\nu_R} \leq m_u/2$~~   
~~via higher dim. operator~~

Not enough moderate the problem

$$\text{Br}(u \rightarrow 2a) \simeq \left[ 1 + 24 \left( \frac{m_{\nu_R}}{m_u} \right)^2 \beta_f^3 \right]^{-1}$$

$\approx 45\%$



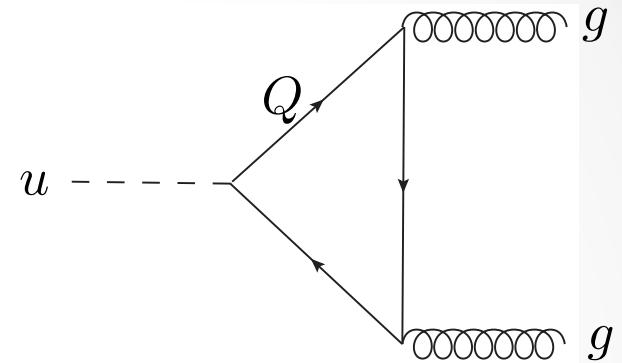
# Coupling with vector-like “quarks”

◎Interaction btwn u and “quarks”

[ex:Kim et.al ('08)]

$$\Delta W = y_Q u Q \bar{Q}$$

(  $Q$ : 5 rep. of  $SU(5)$ ,  $\bar{Q}$ : 5\* rep. )



◎Decay channel of u

[ex:Chun et.al('00)]

$$\Gamma(u \rightarrow gg) \simeq \frac{N_q^2 \alpha_s^2}{144\pi^3} \frac{m_u^3}{\langle u \rangle^2}$$

$$\rightarrow \frac{\Gamma(u \rightarrow gg)}{\Gamma(u \rightarrow 2a)} = \frac{4N_q^2 \alpha_s^2}{9\pi^2}$$

- To overcome  $u \rightarrow 2a$ , we should introduce

$$N_q > 100$$

Huge number of “quarks”!!



[ex:Morrissey et.al ('05)]

Gauge coupling will blow up below the GUT scale!

# Possible solutions

[ H.N & Y.Shimizu ('12) ]

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Energy transfer from u complete before BBN?

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100 flavors of "quarks"

Breaks pGCU below GUT scale

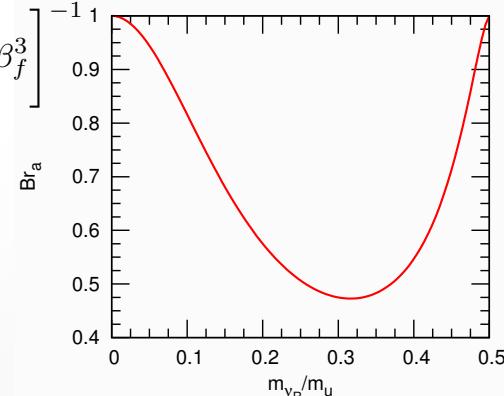
[ex:Morrissey et.al ('05)]

1) Light RH neutrino  $m_{\nu_R} \leq m_u/2$   
via higher dim. operator

Not enough moderate the problem

$$\text{Br}(u \rightarrow 2a) \simeq \left[ 1 + 24 \left( \frac{m_{\nu_R}}{m_u} \right)^2 \beta_f^3 \right]^{-1/2}$$

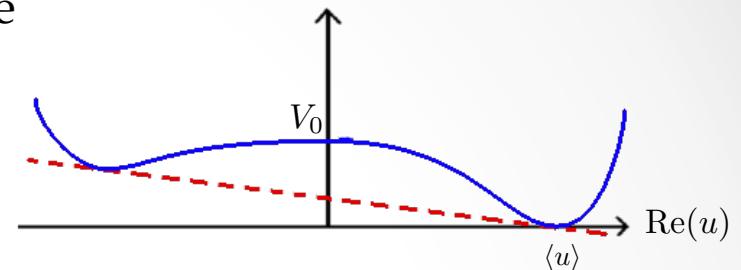
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# Explicit breaking term

- ◎ To kinematically forbid  $u \rightarrow 2a$ , we assume

$$\Delta\mathcal{L} = -\kappa(u + u^*)$$



- ◎ Mass of circumferential comp. of  $u$

$$m_a^2 = \frac{\kappa}{\langle v \rangle} \quad \text{If } \kappa > \frac{m_u^2 \langle u \rangle}{4}, \text{ } u \rightarrow 2a \text{ forbidden kinematically!}$$

- In addition, we introduce  $uQ\bar{Q}$  coupling

$$\Gamma_{\text{tot}} \simeq \Gamma(u \rightarrow gg) \simeq \frac{N_q^2 \alpha_s^2}{144\pi^3} \frac{m_u^3}{\langle u \rangle^2} \quad [\text{ex:Chun et.al ('00)}]$$

→

$$T_R^{(sec)} \simeq 0.45 \sqrt{\Gamma_{\text{tot}} M_p}$$

$$\simeq 6 \text{ MeV} \left( \frac{m_u}{10^3 \text{ GeV}} \right)^{3/2} \left( \frac{\langle u \rangle}{3 \times 10^{12} \text{ GeV}} \right)^{-1}$$

**Energy transfer from  $u$  into SMs can complete  
before BBN begins**

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[ H.N & Y.Shimizu ('12) ]

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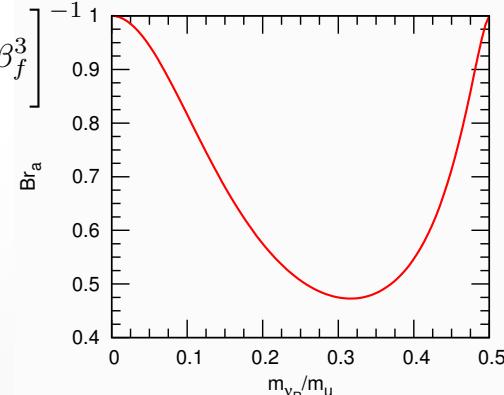
Not enough moderate the problem

$u \rightarrow 2a$  can be forbidden  $m_a^2 = \frac{\kappa}{\langle u \rangle} > m_u^2$

&  $T_R^{(sec)} \simeq \text{few MeV}$  ( $u \rightarrow gg$ )

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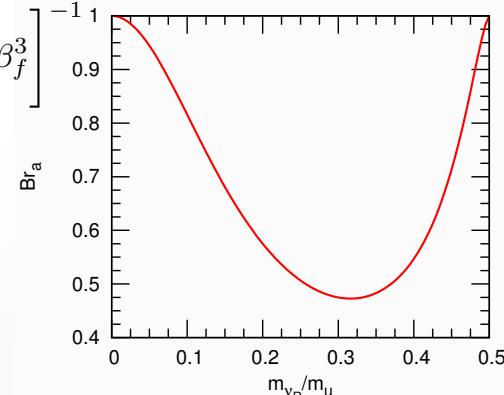
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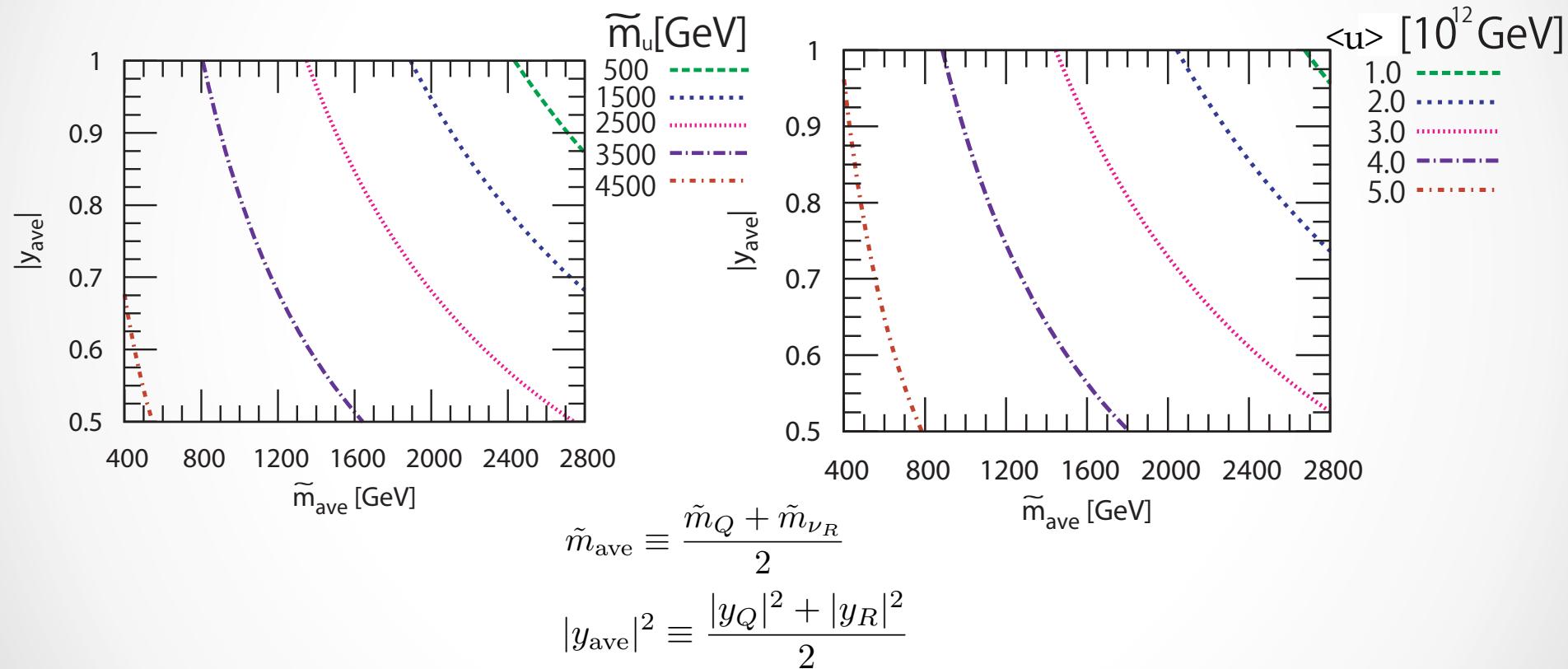
Applicable to thermal inflation by domination of flavon

# Realization of thermal inflation

[ H.N & Y.Shimizu ('12) ]

◎Contours satisfying  $T_R^{(sec)} \simeq \text{few MeV}$

( $\Leftrightarrow \Delta = 10^{20}$ ) ( $\leftarrow$  Primary moduli diluted enough)



Thermal inflation scenario can realize  
by  $u$  domination in SUSY discrete flavour model

# Summary

- Study the thermal evolution of pseudo moduli flavon in SUSY discrete flavour symmetry
  - Obtain analytic expression of VEV of flavon
  - Flavon can dominate the universe at  $\tilde{m}_u < T < V_0^{1/4}$
- **Energy transfer from flavon does not complete before BBN** ( at least minimal framework )
  - Br of  $u \rightarrow 2a$  dominate the decay process
  - Should introduce linear potential into lagrangian
- Domination by  $u$  can be applied into
  - thermal inflation scenario
- Apply to the continuous flavour symmetry ??