

ニ₁-トリノとグ-ジ-ノ混合に

もとづいてニ₁-トリノ質量

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1. Introduction
2. Model = extra $U(1) =$
3. Various issues ← 省略?
4. Summary

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1. Introduction

solar neutrino
atmospheric neutrino } \Rightarrow large mixing

large mixing 的起源? \leftarrow quark sector
small mixing

$$V^{(MNS)} = L_e^+ U_e$$

- charged leptons 的起源 \oplus SU(5), Froggatt-Nielsen
- neutrino 的起源

可能性 \rightarrow 1, 1, 1 的 sector 的 mass matrix

\Rightarrow almost democratic form

$$M \sim m \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$$

rank of $M > 1$ 的起源?

order one coefficients 的 重要性

\leftarrow 物理的背景?



Supersymmetry

\oplus

extra U(1) sym.

gauge hierarchy problem

string a low energy effective model 1: 99 < 100.

neutrino sector 1: large mixing 的起源.

* R-parity violation

R-parity $R_p = (-1)^{3B+L+2S}$

- superparticles -1
 - ordinary particles +1
- R_p mixing 19.8%

neutral fermion
 neutrino (ν_α) - neutralino ($\tilde{\nu}_\alpha, \tilde{w}, \tilde{z}, \tilde{H}_1^0, \tilde{H}_2^0$)

relevant int. to mixing

- $W_{R^0} \supset \epsilon_\alpha L_\alpha H_u$: explicit R_p no $\epsilon_\alpha \tilde{L}_\alpha \tilde{H}_u^0$
- $i\sqrt{2}g_a (\tilde{U}_\alpha^\dagger T^a T^b L_\alpha - \tilde{J}_\alpha^\dagger T^a T^b \tilde{H}_\alpha)$
 $\langle \tilde{U}_\alpha \rangle \neq 0$ spontaneous R_p

↓

$$(\nu_e \nu_\mu \nu_\tau) \begin{pmatrix} \sqrt{2}g_2 \langle \tilde{U}_e \rangle & \sqrt{2}g_1 \langle \tilde{U}_e \rangle & \epsilon_e \\ \sqrt{2}g_2 \langle \tilde{U}_\mu \rangle & \sqrt{2}g_1 \langle \tilde{U}_\mu \rangle & \epsilon_\mu \\ \sqrt{2}g_2 \langle \tilde{U}_\tau \rangle & \sqrt{2}g_1 \langle \tilde{U}_\tau \rangle & \epsilon_\tau \end{pmatrix} \begin{pmatrix} -\tilde{w}_3 \\ \tilde{z} \\ \tilde{H}_2^0 \end{pmatrix}$$

pot. steady $\langle \tilde{U}_\alpha \rangle \propto \epsilon_\alpha$

gaugino mass $\gg \langle \tilde{U}_\alpha \rangle$ mixing 19.8%
 seesaw $\sim M_{ij}^\nu \propto \frac{\langle \tilde{U}_i \rangle \langle \tilde{U}_j \rangle}{\Lambda^2}$

nonzero mass eigenvalue $\sim 1/\Lambda^2$

mass perturbation $\propto \frac{1}{\Lambda^2} \Rightarrow$ one-loop effect

tree level $\tilde{\nu}$ mixing & mass eigenvalues?

2. A model

extra $U(1)$ model (TeV 領域)

- string model \sim additional $U(1)$'s
- μ -problem a fit model 2017 2.6 L311.

= constraints =

- precision measurement

$$\sim M_{Z'} \geq 600 \text{ GeV}, \quad \alpha - \alpha' \text{ mixing} \leq 10^{-3}$$

- precision measurement atomic parity violation \rightarrow extra $U(1)$ favor? Langacker et al.

generation dependent $U(1)$ flavor diagonal

neutrino-gaugino mixing $\sqrt{2} \tilde{g} \times \tilde{b}_\alpha \langle \tilde{V}_\alpha \rangle$

\sim at tree level nonzero mass eigenvalues: 2701 !

- neutrino oscillation phenomena?
- other features?

《 \tilde{g} と \tilde{b} 》

- neutrino mass — TeV 領域 $U(1)$ の影響
- quark mass — Froggatt-Nielson mechanism
- charged leptons

extra $U(1)_X$ (T-odd sector) (lepton sector only)

$l_L = (\delta_I, \delta_{II}, \delta_{III})$, $\bar{l}_R = (-\delta_I, -\delta_{II}, -\delta_{III})$ — Toy model
 H_1, H_2 : zero charge. — flavor identification is not.

• charged lepton

$m_e = \begin{pmatrix} * & * & 0 \\ * & * & 0 \\ 0 & 0 & * \end{pmatrix} \sim$ diagonal in basis.

• neutrino

$\langle \tilde{\nu}_e \rangle = \langle \tilde{\nu}_\mu \rangle = \langle \tilde{\nu}_\tau \rangle \equiv u$

$M = \begin{pmatrix} 0 & m^T \\ m & M \end{pmatrix}$, $m = \begin{pmatrix} a_2 & a_1 & b \\ a_2 & a_1 & b \\ a_2 & a_1 & c \end{pmatrix}$, $M = \begin{pmatrix} M_L & & 0 \\ & M_1 & \\ 0 & & M_X \end{pmatrix}$

$a_2 \equiv \frac{g_2}{\sqrt{2}} u$, $b \equiv \sqrt{2} g_X \delta_{II} u$, $c \equiv \sqrt{2} g_X \delta_{III} u$

$M^U = m^T M^{-1} m = \begin{pmatrix} m_0 + \epsilon^2 & m_0 + \epsilon^2 & m_0 + \epsilon \delta \\ m_0 + \epsilon^2 & m_0 + \epsilon^2 & m_0 + \epsilon \delta \\ m_0 + \epsilon \delta & m_0 + \epsilon \delta & m_0 + \delta^2 \end{pmatrix}$

$m_0 = \frac{g_2^2 u^2}{2M_L} + \frac{g_1^2 u^2}{2M_1}$, $\epsilon = \frac{g_X g_2 u}{\sqrt{M_X}}$, $\delta = \frac{g_X g_{II} u}{\sqrt{M_X}}$

diagonalization matrix U

$N_\alpha = U_{\alpha i} \tilde{N}_i$

$U = \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \cos \theta & \frac{1}{\sqrt{2}} \sin \theta \\ -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \cos \theta & \frac{1}{\sqrt{2}} \sin \theta \\ 0 & -\sin \theta & \cos \theta \end{pmatrix}$

mass eigenstate

charged lepton diagonal

$\sin^2 2\theta = \frac{\delta(m_0 + \epsilon \delta)^2}{(m_0 + 2\epsilon^2 - \delta^2)^2 + \delta(m_0 + \epsilon \delta)^2}$

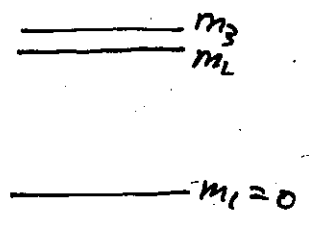
$\left. \begin{aligned} m_{2,3} &= \frac{1}{2} \left\{ (3m_0 + 2\epsilon^2 + \delta^2) \mp \sqrt{(m_0 + 2\epsilon^2 - \delta^2)^2 + \delta(m_0 + \epsilon \delta)^2} \right\} \\ m_1 &= 0 \end{aligned} \right\}$

$$P_{\alpha \rightarrow \beta}^{(L)} = \delta_{\alpha\beta} - 4 \sum_{i < j} U_{\alpha i} U_{\beta i} U_{\alpha j} U_{\beta j} \sin^2 \left(\frac{\Delta m_{ij}^2 L}{4E} \right)$$

(α, β)	(i, j)	$-4 U_{\alpha i} U_{\beta i} U_{\alpha j} U_{\beta j} (\equiv A)$
(I, II)	(1, 2)	$\cos^2 \theta$ (A)
	(1, 3)	$\sin^2 \theta$ (B)
	(2, 3)	$-\sin^2 \theta \cos^2 \theta$ (C)
(I, III)	(2, 3)	$2 \sin^2 \theta \cos^2 \theta$ (D)
(II, III)	(2, 3)	$2 \sin^2 \theta \cos^2 \theta$ (E)

$\vec{P}_2 \approx \vec{V}_3$: almost degenerate case

inverse hierarchy



(atm) $2 \times 10^{-3} \text{ eV}^2 \lesssim \Delta m_{12}^2 \lesssim \Delta m_{13}^2 \lesssim 6 \times 10^{-3} \text{ eV}^2$

(solar) $10^{-10} \text{ eV}^2 \lesssim \Delta m_{23}^2 \lesssim 1 \text{ eV}^2 < 10^{-8} \text{ eV}^2$

\hookrightarrow solution dep. 12 $\theta_{12} \neq 0$

$(I, II, III) \implies (\tau, \mu, \theta)$

$$U_{MNS} = \begin{pmatrix} 0 & -\sin \theta & \cos \theta \\ -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \cos \theta & \frac{1}{\sqrt{2}} \sin \theta \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \cos \theta & \frac{1}{\sqrt{2}} \sin \theta \end{pmatrix}$$

$m_1, \text{ etc}$

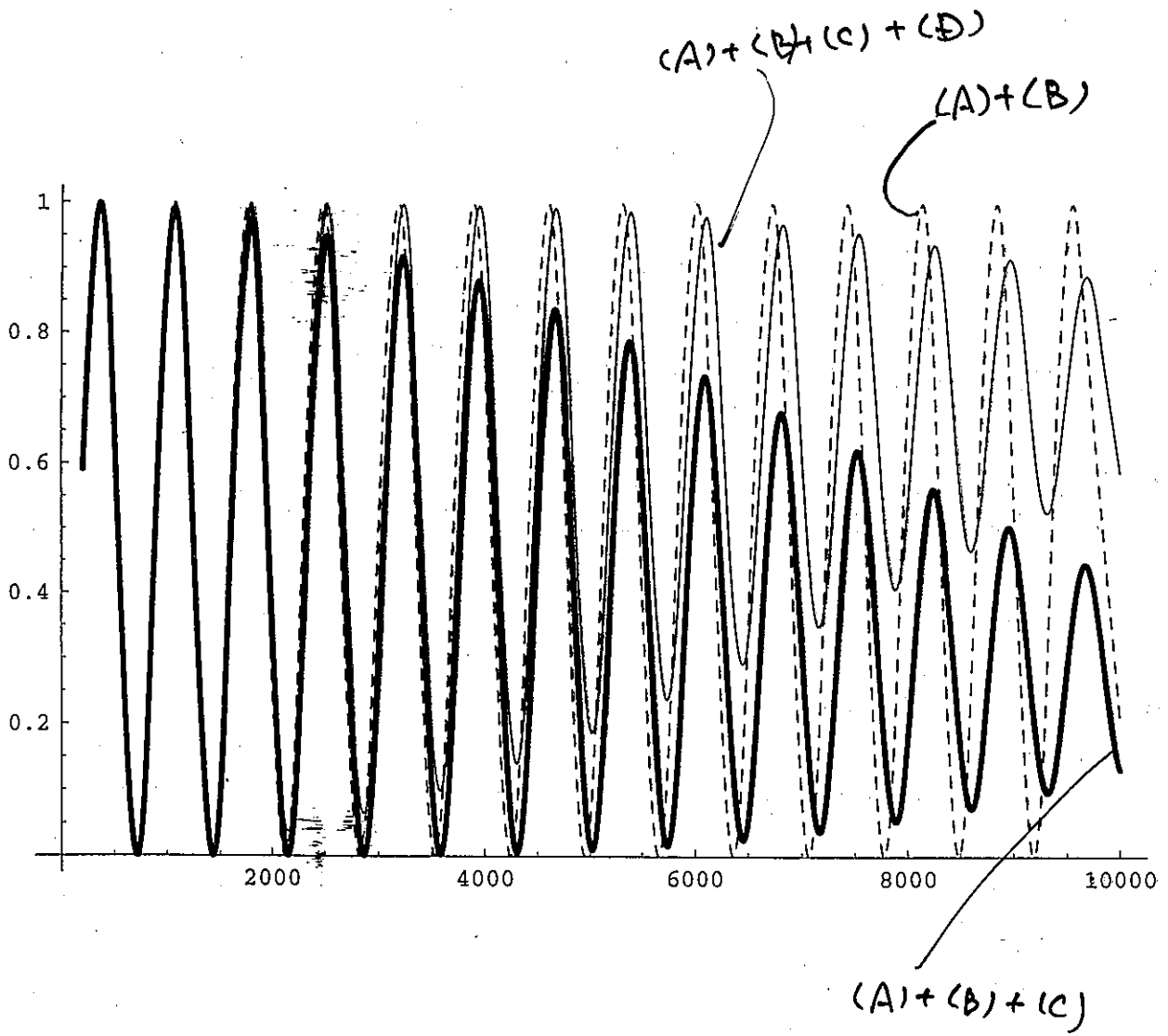
(atm) $\nu_\mu \rightarrow \nu_\tau$ (A) + (B)
 $\Delta m_{12}^2 \approx \Delta m_{13}^2$

(solar) $\nu_e \rightarrow \nu_\mu$ (E)
 $\nu_e \rightarrow \nu_\tau$ (D)
 $\Delta m_{23}^2 = \dots$

$\sin^2 2\theta$

$\sin^2 2\theta \sim 10^{-2}$ SMA
 $\sin^2 2\theta \sim 1$ LMA
 LOW
 VO

Δm_{23}^2 dup



- CHOOZ constraint (power station, long baseline)
 $\mu_e \rightarrow \nu_{3e}$ with Δm_{12}^2 or Δm_{13}^2 $L \sim 1 \text{ km}, E \sim 3 \text{ MeV}$

$\theta \sim U_{e1} \sim \sqrt{1/2} \approx 0.7$ $U_{e1} = 0$ o.k

- mode (c) $\mu_\mu \rightarrow \nu_2$ if $\sin^2 2\theta \approx 1$
 irrelevant to short baseline exp.

but $\Delta m_{23}^2 \sim 10^{-4} \text{ eV}^2$ (LMA)

$L \sim 2000 \text{ km}$ long baseline exp.

(Fig)

- neutrinoless double β -decay $\phi_j = 0 \approx 12$

$m_2 \sim m_3$

$$|M_{ee}| = \left| \sum_j |U_{ej}|^2 e^{i\phi_j} m_j \right| = (m_2 \sin^2 \theta + m_3 \cos^2 \theta) \sim m_3$$

\Downarrow

$|M_{ee}| \sim 0.04 - 0.08 \text{ eV}$ indep. of $\sin \theta$

✦ realization of oscillation parameters

M_A, g_A, g_x, u : parameters

universal gaugino mass M_0

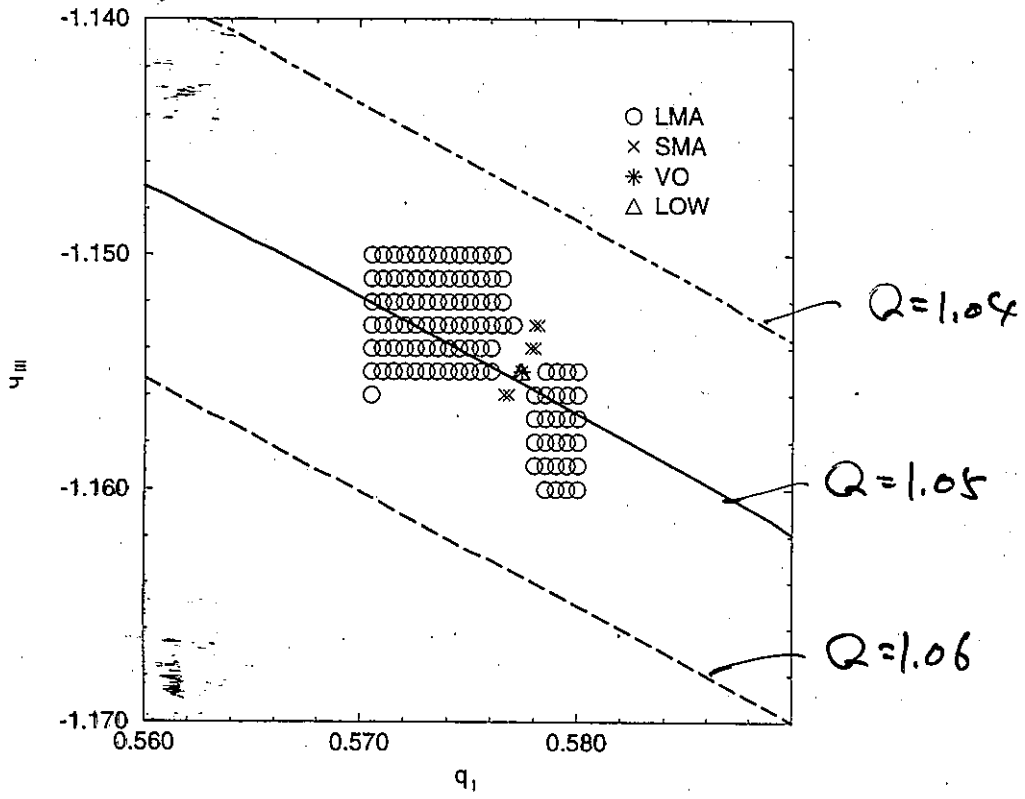
one-loop RGE

$$M_2(\mu) = \frac{M_0}{g_0^2} g_2^2(\mu), \quad M_1(\mu) = \frac{5}{3} \frac{M_0}{g_0^2} g_1^2(\mu)$$

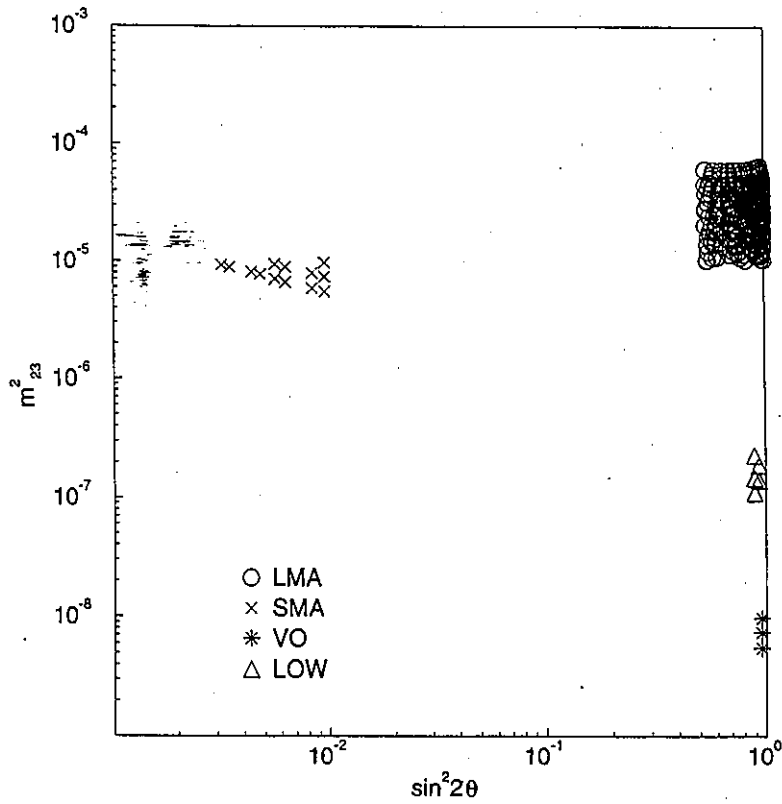
M_x, g_x : M_1, g_1 と同様に μ 依存

(U(1)_x Kac-Moody level $a \pm b/g$)

(a)



(b)



$$m_{2,3} = \frac{3}{5} \left(2 + 2g_I^2 + g_{II}^2 \mp \sqrt{(2 + 2g_I^2 + g_{II}^2)^2 - \frac{16}{3}(g_I - g_{II})^2} \right) \frac{g_U^2 u^2}{M_0}$$

$$\sin^2 2\theta = \frac{\rho(2 + 3g_I g_{II})^2}{(2 + 6g_I^2 - 3g_{II}^2)^2 + \rho(2 + 3g_I g_{II})^2} \quad \text{overall factor}$$

atmospheric neutrino $\sim 0.017 \text{ eV} \lesssim \frac{g_U^2}{M_0} u^2 \lesssim 0.023 \text{ eV}$

(EX) $M_0 \sim 100 \text{ GeV} \Rightarrow u \sim 60-70 \text{ GeV}$
 $g_U \sim 0.72$

$\Delta m^2, \sin^2 2\theta \Rightarrow g_I, g_{II}$ (Fig.)

$$\Delta m_{23}^2 \propto \sqrt{(2 + 2g_I^2 + g_{II}^2)^2 - \frac{16}{3}(g_I - g_{II})^2}$$

$m_{2,3}$ の 1/2 全分 (2) $\left(g_I = \frac{1}{\sqrt{3}}, g_{II} = -\frac{2}{\sqrt{3}} \right) \left(\sum_{\alpha} g_{\alpha} = 0 \right)$
 = 4/5 5/3 ずつ

LMA: $U(1)_X$ charge tuning is still needed mild V.O.K.

(iii) parameter $\frac{1}{2} g_I, g_{II}$ (gauge coupling)
 \sim factor a 標準論より $\frac{1}{2} g_I$

$U(1)_X$ charge \sim mass a $\pm \epsilon$ t
 mixing is 反相

Froggatt-Nielsen $\sim \frac{1}{2} g_I$ of low energy $U(1)_X$

charge is a control is 標準論より
 $\frac{\langle \Theta \rangle}{M_{pl}} \sim 1$

3. Various issues

(1) anomaly free $U(1)_X$?

anomaly free condition \rightarrow consistent with (g_2, g_2) ?

additional fields $SU(2)_L \times U(1)_Y$

$2_0, 1_{\pm 1}, 4(1_0)$

- anomaly free conditions
- $2_0, 1_{\pm 1}$ massive at T_{EW} / \hat{R}^2 etc.

$$\Downarrow$$

$$f(g_1, g_2, Q) = 0 \quad Q: \text{charge of } \frac{1_0}{(2, 2, 0)}$$

consistent \rightarrow $\tau \leftrightarrow \mu$ etc.

(2) Z' nonuniversal coupling \rightarrow FCNC?

$U(1)_X$: flavor diagonal but generation dep.

\hookrightarrow in general FCNC dangerous
coherent μ - e conversion, $\tau \rightarrow 3e, 3\mu, \mu \rightarrow e\tau, \dots$

Z' interaction in mass eigenstates

$$\mathcal{L}_{Z'} = -g_1 \left[\frac{g_2}{g_1} \cos^2 \theta \ J_{(A)}^{\mu} - \sin^2 \theta \ J_{(1)}^{\mu} \right] Z'_{\mu}$$

$$J_{(A)}^{\mu} = \sum_{ij} \left[\bar{L}_i B_{ij}^{\mu L} L_j + \bar{L}_i B_{ij}^{\mu l} l_j + \bar{R}_i B_{ij}^{\mu R} R_j \right]$$

$$B_{ij}^{\mu} = V^{\mu\dagger} \text{diag}(g_2, g_2, g_1) V^{\mu}$$

$$V^{\mu\dagger} m_{\nu}^{\mu} V^{\mu} = \text{diag.} \quad m_e = \begin{pmatrix} * & 0 & 0 \\ 0 & * & * \\ 0 & * & * \end{pmatrix}$$

$$\left. \begin{aligned} m_{\mu\mu} = m_{e\tau} = 0 &\Rightarrow B_{12}^{Lc, R} = B_{13}^{Lc, R} = 0 \\ g_{\mu} = g_{\tau} &\Rightarrow B_{23}^{Lc, R} = 0 \end{aligned} \right\}$$

nonuniversal coupling \Rightarrow FCNC : O.K

extended neutralino sector \sim FCNC

MSSM 2nd bound $(M \in \tau, \beta)$ soft supersym parameters
 \sim O.K.

$M_{Z'} \gtrsim 600$ GeV. Z - Z' mixing $\leq 10^{-3}$
 no phenomenological problem

(3rd) structure VEV $\sim O(10^2 \text{ GeV})$?

e.g. \Rightarrow bilinear R-parity violating terms $\in L\alpha H_2$

potential minimization

$$u \sim \frac{\delta E (\mu \langle H_1 \rangle + B_e \langle H_2 \rangle)}{3(g_1^2 + g_2^2) (\langle H_1 \rangle^2 - \langle H_2 \rangle^2) + 2g_+^2 \left(\frac{D}{\alpha} g_w\right) (g_1 \langle H_1 \rangle^2 + g_2 \langle H_2 \rangle^2) + 6m^2}$$

$$E \ll \mu, m^2, B_e \sim M_w$$

\hookrightarrow small u ($\neq 0$) B_e stability ?

detailed study $\tau \mu \mu \tau$.

4. Summary

1) supersym. & neutrino mass a 問題 3"17 17 可能.
 R-parity violation & generation dep. low energy U(1)
 ↳ parameter a chiral model LMA 可能

2) sneutrino VEV a 非ゼロ??

3) quark sector & U model a 問題 ^{anomalous} U(1)_{F1} × U(1)_{F2}
 • quark sector / charged lepton { Froggatt-Nielsen high energy breaking
 ↳ charge 17 17 可能
 • neutrino ~~R-parity~~ low energy breaking
 ↳ charge 17 mass 10 可能
 LMA 3 可能 model 10 2" 2 2 5

4) mass matrix form
 ↳ scale up { ordinary seesaw
 Froggatt-Nielsen
 hep-ph/0104187

O(1) coefficient a 重要物.
 model 17 17 可能 hep-ph/0105223

sterile neutrino a 重要物
 LMA 3 可能 17 17 可能 ↳ LMA 100% favor

100

100

100

100

100

100

100

100