

太陽ニュートリノ問題の解は 素粒子理論にとって何を意味するか

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1. はじめに

Solar Neutrino Deficit

V. Bangor, K. Whisnant, R.J.N. Phillips
PRD 24 (1981) 538

Maximal Mixing θ_{eu}^0 in vacuum

MSW 効果 1985

Small Mixing θ_{eu}^0

Atmospheric Neutrino Deficit

Maximal (?) Mixing $\theta_{\mu\tau}^0$ 1998

Model Buildings

5 options for Solar Neutrino Deficit

- SMA MSW • LMA MSW • LOW
- Just-50 • sterile

大角度フレバー混合に対する

心理的抑圧からの解放

Supn - Kam 2000

Emerging default option

3 family, Bi-Maximal (LMA MSW)



- Model の再検討のはじまり
- KamLAND への期待
as well as SNO

GUT

フル-バー対称性



LMA MSW 解

2. 大角度フレーバー混合と 質量行列の構造

ニュートリノフレーバー混合行列 (MNS 行列)

$$U_{MNS} \equiv L_E^\dagger L_\nu$$

$$\left. \begin{aligned} L_E^\dagger M_E R_E &= M_E^{diag} \\ L_\nu^T M_\nu L_\nu &= M_\nu^{diag} \end{aligned} \right\} \begin{array}{l} \text{in some preferred} \\ \text{basis given by underlying} \\ \text{theory of that model} \end{array}$$

o Single Large Mixing (Atmospheric Neutrinos) の場合

Large Mixing from M_E or M_ν

M_E : Democratic

Lopsided

solar \rightarrow

$$L_E^\dagger: \begin{pmatrix} \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} & LR \\ \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} & 0 \\ \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{6}} & \frac{2}{\sqrt{6}} \\ \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} \end{pmatrix} \end{pmatrix}$$

$$\begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{pmatrix} LR$$

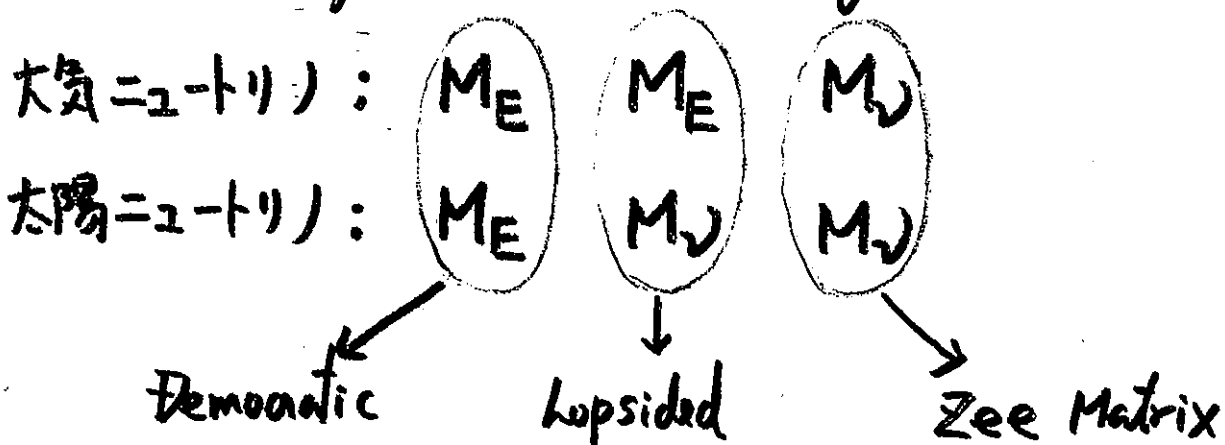
$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix} \\ 0 & \begin{pmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix} \end{pmatrix}$$

M_ν : See-Saw $-m_D^T M_R^{-1} m_D = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix}$

Zee Mass Matrix $\begin{pmatrix} 0 & 1 & 1 \\ 1 & 0 & \epsilon \\ 1 & \epsilon & 0 \end{pmatrix}$

○ Bi-large (Maximal) Mixings の場合

5



LMA MSW 解

$$\Delta m_{21}^2 = (2 \sim 20) \times 10^{-5} \text{ eV}^2$$

$$\sin^2 2\theta_{12} = 0.6 \sim 0.97$$

$$\frac{\Delta m_{21}^2}{\Delta m_{atm}^2} = (1 \sim 10) \times 10^{-2} \approx \lambda^2 \sim \lambda^3$$

$$\sqrt{\frac{\Delta m_{21}^2}{\Delta m_{atm}^2}} \approx \frac{m_{\nu 2}}{m_{\nu 3}} \approx \lambda \sim \lambda^{1.5} \approx 10$$

$$\frac{m_s}{m_b} \approx \lambda^2$$

$$\frac{m_c}{m_t} \approx \lambda^4$$

$$\frac{m_\mu}{m_\tau} \approx \lambda^2$$

3 Bi-Maximal Mixings & SO(10) GUT

Albright, Babu, Barr PRL 81 (1998) 1167
 hep-ph/9906299, 0002155

Minimal SO(10) $16_i, 16_j, 10_H$ SO(5)
↓

$16_i (10_{u, \nu^c, d, e^c} \quad 5^*_{d^c, e, \nu} \quad 1_{\nu^c})_L$

$m_N^{\text{Dirac}} = m_U \propto m_D = m_E$ No mixings

$(16_3, 16_3) 10_H, (16_2, 16_3) 10_H, 45_H$

$[16_3, 16_H] [16_2, 16'_H] [16_1, 16_2] [16_H, 16'_H]$
 $[16_1, 16_3] [16_H, 16'_H]$

$$M_E = \begin{pmatrix} 0 & \delta & \delta' \\ \delta & 0 & \delta + \epsilon \\ \delta' & -\epsilon & 1 \end{pmatrix} \quad \begin{aligned} \epsilon &\approx 0.14 \\ \delta &\approx \delta' \approx 0.008 \\ \delta &\approx 1.8 \end{aligned}$$

Quarks 1, 2, 3.

$$\left. \begin{aligned} m_s^0 / m_b^0 &\approx \frac{1}{3} \epsilon \frac{\delta}{1 + \delta^2} \\ V_{cb}^0 &\approx \frac{1}{3} \epsilon \frac{\delta^2}{1 + \delta^2} \\ V_{us} &\approx -\frac{\delta}{\sqrt{1 + \delta^2}} \end{aligned} \right\} \begin{aligned} |V_{cb}| &= \frac{m_s^0}{m_b^0} \delta \\ |V_{us}| &= \frac{\delta}{\sqrt{1 + \delta^2}} \end{aligned}$$

$$M_N^{\text{Dirac}} = \begin{pmatrix} \eta & 0 & 0 \\ 0 & 0 & -\epsilon \\ 0 & \epsilon & 1 \end{pmatrix} M_D \quad SO(10)$$

$$W_{\text{Yukawa}} \ni 1_3^c 1_3^c V_M + 1_1^c 1_2^c \cdot V_M$$

$$M_R = \begin{pmatrix} 0 & A & 0 \\ A & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} \Lambda_R$$

after See - Saw

$$M_\nu = m_0 \begin{pmatrix} -(\frac{\eta}{A})^2 \epsilon^2 & (\frac{\eta}{A}) \epsilon^2 & 0 \\ (\frac{\eta}{A}) \epsilon^2 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$\exists L \quad \eta/A \ll 1 \rightarrow \text{maximal mixing}$

$$\Delta m_{21}^2 = 2 |\eta/A|^3 \epsilon^4 (M_D/\Lambda_R)^2$$

$$\Delta m_{21}^2 \approx 4 \times 10^{-10} \text{ eV}^2 \quad \text{if } \eta/A \approx 0.05$$

$$\Delta m_{21}^2 \approx 2 \times 10^{-5} \text{ eV}^2 \quad \text{if } |\eta/A| \approx 1.8$$

$$\text{if } L, \Delta m_{32}^2 \approx 3.5 \times 10^{-3} \text{ eV}^2 \quad \text{if } L \neq 0$$

$$(B1) \quad \Delta m_{21}^2 \approx 2 \times 10^{-5} \text{ eV}^2$$

$$\sin^2 2\theta_{MNS} \approx 0.82 \quad \sin^2 2\theta_{eM} \approx 0.43 !!$$

Nomura, Yanagida, PR D59 (1999) 019303 8
 Nomura, Sugimoto, hep-ph/9903334, PR D61 (2000) 093403

$$\psi_3(16) = 10_3 + 5_3^* + N_3$$

$$\psi_2(16) = 10_2 + 5_2^* + N_2$$

$$\psi_1(16) = 10_1 + 5_1^* + N_1$$

$$\psi(10) = 5_4 + 5_4^*$$

$$W = \sum_{i=1}^3 f_i \psi_i(16) \psi(10) \langle X(16) \rangle$$

10^{15} GeV

$$W = h_i \psi_i(16) \psi_i(16) H(10)$$

5_4^* is $H(10)$ is for Yukawa Coupling τ ($\tau = \tau_0$)

$$W = k H(10) \bar{H}(16^*) \bar{\chi}(16^*) + M H(16) \bar{H}(16^*)$$

$H(10)$ & $H(16)$ is $i\mathbb{R}^2$!

$$\tilde{5}_H^* = \cos \theta 5_{H(10)}^* + \sin \theta 5_{H(16)}^*$$

$$W = \sum_{i=1}^3 g_i \psi_i(16) \psi(10) H(16)$$

$$W_{\text{eff}} = \sin \theta \sum_{i=1}^3 g_i 10_i 5_4^* \tilde{5}_H^*$$

$$+ \cos \theta \sum_{i=1}^3 h_i 10_i 5_i^* \tilde{5}_H^*$$

} Yukawa
Coupling
of $\tilde{5}_H^*$

$$W_{\text{eff}} = \cos\theta (10_1, 10_2, 10_3) \begin{pmatrix} 0 & g_1 \tan\theta & 0 \\ h_2 & g_2 \tan\theta & 0 \\ 0 & g_3 \tan\theta & h_3 \end{pmatrix} \begin{pmatrix} 5_2^* \\ 5_4^* \\ 5_3^* \end{pmatrix} \quad 5_H^*$$

$$M_D = M_E^T = m_t \begin{pmatrix} 0 & x & 0 \\ m_c/m_t & y & 0 \\ 0 & z & 1 \end{pmatrix} \times \frac{\cos\theta}{\tan\beta}$$

$$x = \frac{g_1}{h_3} \tan\theta, \quad y = \frac{g_2}{h_3} \tan\theta, \quad z = \frac{g_3}{h_3} \tan\theta$$

$$x \approx m_c/m_t, \quad y \approx \sqrt{m_c/m_t}, \quad z \approx 1 \Rightarrow \text{nice fits}$$

$$\theta_{uz} \approx \pi/4 \text{ from } z=1$$

Neutrino Sector is どうなるか? 5_4^* never couples to N_i in $4_2(16)$

$$W = \sum_{i=1}^3 K_i \psi_i(16) \psi(10) H(10) \frac{\bar{\chi}(16^*)}{M_G} \quad 5_H$$

$$M_\nu^{\text{Dirac}} = m_t \begin{pmatrix} 0 & \delta_1 & 0 \\ m_c/m_t & \delta_2 & 0 \\ 0 & \delta_3 & 1 \end{pmatrix} \quad \delta_i = \frac{K_i}{h_3} \frac{\langle \chi(16) \rangle}{M_G}$$

$$\delta_1 \approx \delta_3 \approx 0 \quad \delta_2 \approx m_c/m_t$$

$$W = \delta_{ij} \frac{1}{M_G} \psi_i(16) \psi_j(16) \bar{\chi}(16^*) \bar{\chi}(16^*)$$

$$(M_R)_{ij} = \frac{\langle \bar{\chi}(16^*) \rangle^2}{M_G} \delta_{ij} \propto \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

??? ?

$$M_\nu = \frac{(m_t)^2}{M_N} \begin{pmatrix} \gamma^2 & \delta_2 \gamma & 0 \\ \delta_2 \gamma & \delta_1^2 + \delta_2^2 + \delta_3^2 & \delta_3 \\ 0 & \delta_3 & 1 \end{pmatrix} \quad \gamma = \frac{m_c}{m_t}$$

As $\delta_1 \approx \delta_3 \approx 0 \quad \delta_2 = \gamma \quad \epsilon \quad \epsilon \quad \epsilon$

$$M_\nu \propto \begin{pmatrix} \gamma^2 & \gamma^2 & 0 \\ \gamma^2 & \gamma^2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad \theta_{eu} = \frac{\pi}{4} !$$

$$U_{MNS} = L_E^+ L_\nu \approx \begin{pmatrix} 1/\sqrt{2} & -1/\sqrt{2} & \epsilon \\ 1/2 & 1/2 & -1/\sqrt{2} \\ 1/2 & 1/2 & -1/\sqrt{2} \end{pmatrix} \quad \text{Bi-Maximal}$$

Neutrino Masses

$$m_2^\nu / m_3^\nu \approx \delta_2^2 \approx \frac{m_c^2}{m_t^2} \approx 5 \times 10^{-5}$$

$$\Delta m_{21}^2 \approx 10^{-11} \text{ eV}^2 \quad \longrightarrow \text{Just-So solution}$$

However

$$(M_\nu)_{ij} \propto \begin{pmatrix} \epsilon^4 & \epsilon^3 & \epsilon^2 \\ \epsilon^3 & \epsilon^2 & \epsilon \\ \epsilon^2 & \epsilon & 1 \end{pmatrix} \quad \text{NSI}$$

$$\Delta m_{21}^2 \approx 10^{-5} \text{ eV}^2 \quad \text{or } \epsilon^2 \text{ or } \epsilon$$

LMA MSW

4 Bi-Maximal Mixings と Z_3 -対称性 Prototype と Z_3 の Democratic Matrix

"flavor - democratic" $S_{3L} \times S_{3R}$

$$M_{FD} = \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}_{LR} m \quad \begin{array}{l} \text{rank 1} \\ (0, 0, 3)m \end{array}$$

\Downarrow

$$U_{FD} = \begin{pmatrix} 1/\sqrt{2} & 1/\sqrt{6} & 1/\sqrt{3} \\ -1/\sqrt{2} & 1/\sqrt{6} & 1/\sqrt{3} \\ 0 & -2/\sqrt{6} & 1/\sqrt{3} \end{pmatrix}$$

$$M_E = C_E M_{FD} + M_E^{\text{break}}$$

$S_{3L} \times S_{3R}$

$$M_\nu = C_\nu I + \underbrace{C'_\nu}_{\text{small}} M_{FD} + M_\nu^{\text{break}}$$

S_{3L} Majoranas

$$m_{\nu_1} \approx m_{\nu_2} \approx m_{\nu_3}$$

$$U_{MNS} = L_E^\dagger L_\nu \approx U_{FD} \approx \begin{pmatrix} 1/\sqrt{2} & -1/\sqrt{2} & 0 \\ 1/\sqrt{6} & 1/\sqrt{6} & -2/\sqrt{6} \\ 1/\sqrt{3} & 1/\sqrt{3} & 1/\sqrt{3} \end{pmatrix}$$

$$\sin^2 2\theta_{12} \approx \frac{8}{9} \quad \sin^2 2\theta_{23} \approx 1$$

$$(\text{if}) \sin^2 2\theta_{23} = 1 - \frac{4}{3} \left(\frac{Br}{E} \right)_{21}^2 \approx 1 - \frac{4}{3} \frac{m_e}{m_\mu} \approx 0.99$$

Miura, Takasugi, Yoshimura, hep-ph/0003139 Z_3 symmetry

$O(3)_L \times O(3)_R$ flavor symmetry in the model

$S_{3L} \times S_{3R}$ in the model \Rightarrow flavor democratic for M_θ, M_E

マヨヨヲトニエトリ) M_ν

$$M_\nu = c_\nu \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + c_\nu \gamma \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} S_{3L}$$

Large MNS Mixing $\Rightarrow \gamma \ll 1 \Rightarrow m_{\nu_1} = m_{\nu_2} = m_{\nu_3}$

$\nu_i (i=1 \sim 3)$ Degenerate } unified picture?
 θ_i, E_i Hierarchical }

$O(3)$ flavor symmetry is necessary

$O(3)$ Symmetric Limit

$$\psi_3^{\theta} = (\theta_1, \theta_2, \theta_3)^T \quad \psi_3^L = (\ell_1, \ell_2, \ell_3)^T$$

ν_i : Degenerate Masses

θ_i, E_i are massless

M.T, Watari, Yanagida

PLB 46 (1999) 395

$O(3)$ Breaking

ν_i Degeneracy is lifted

θ_i, E_i have hierarchical masses.

Δm_{ij}^2 are related with m_{θ_i}, m_{E_i} .

$O(3)_L \times O(3)_R$ Flavor Symmetry

$\mathcal{L}_L^i (i=1\sim 3)$ $O(3)_L$ triplet, $\mathcal{E}_R^i (i=1\sim 3)$ $O(3)_R$ triplet

$$\Sigma_{L,R}^{(1)} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix} W_{L,R}^{(1)} \quad \begin{matrix} 3 \times 3 = 1 + 3 + 5 \\ \text{Symmetric} \\ \text{traceless tensors} \end{matrix}$$

$$\Sigma_{L,R}^{(2)} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} W_{L,R}^{(2)} \quad \begin{matrix} (5_L, 1_R) \\ (1_L, 5_R) \end{matrix}$$

Explicit Breakings to avoid unwanted massless Nambu-Goldstone Bosons.

$$\delta_{L,R}^{(1)} \equiv \frac{\Sigma_{L,R}^{(1)}}{M_f} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & -2 \end{pmatrix} \delta_{L,R}$$

$$\delta_{L,R}^{(2)} \equiv \frac{\Sigma_{L,R}^{(2)}}{M_f} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \epsilon_{L,R} \quad \begin{matrix} \delta_{L,R} \leq 1 \\ \epsilon_{L,R} \leq 1 \end{matrix}$$

$$\delta_{L,R} \equiv W_{L,R}^{(1)} / M_f \quad \epsilon_{L,R} \equiv W_{L,R}^{(2)} / M_f$$

$$W = \frac{H^2}{M} \mathcal{L} (1 + \alpha_{(1)} \delta_L^{(1)} + \alpha_{(2)} \delta_L^{(2)}) \mathcal{L}$$

$$\hat{m}_\nu = \frac{\langle H \rangle^2}{M} \left\{ \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + \alpha_{(1)} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix} \delta_L + \alpha_{(2)} \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \epsilon_L \right\}$$

Almost degenerate neutrino masses.

Quarks and charged lepton are still massless. '7

$$\phi_L(3, 1) \quad \phi_R(1, 3) \Rightarrow \text{mass}$$

VEV are determined by superpotential

$$W = Z_L(\phi_L^2 - 3v_L^2) + Z_R(\phi_R^2 - 3v_R^2) \\ + X_L(a^{(i)}\phi_L\delta_L^{(i)}\phi_L) + X_R(a'^{(i)}\phi_R\delta_R^{(i)}\phi_R) \\ + Y_L(b^{(i)}\phi_L\delta_L^{(i)}\phi_L) + Y_R(b'^{(i)}\phi_R\delta_R^{(i)}\phi_R)$$

$X_{L,R}$ $Y_{L,R}$ $Z_{L,R}$ are $O_{3L} \times O_{3R}$ singlets.

Minimizing potential $|F_x|^2 = 0$ $|F_y|^2 = 0$ $|F_z|^2 = 0$

$$\langle \phi_L \rangle = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} v_L \quad \langle \phi_R \rangle = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} v_R$$

For charged lepton,

$$W = \frac{K_Q}{M_f^2} (\bar{e}_R \phi_R) (\phi_L l_L) \bar{H} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} (111)$$

$$\hat{m}_Q = K_Q \left(\frac{v_L v_R}{M_f^2} \right) \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} \langle \hat{H} \rangle$$

assume $v_L \sim v_R \sim M_f$ $m_\tau = 3K_Q \frac{v_L v_R}{M_f^2} \langle \hat{H} \rangle$

Minimizing Potential

$$\phi_L^2 - 3\nu_L^2 = 0 \quad \phi_R^2 - 3\nu_R^2 = 0$$

$$\phi_L \delta_L^{(1)} \phi_L = 0 \quad \phi_R \delta_R^{(1)} \phi_R = 0$$

$$\phi_L \delta_L^{(2)} \phi_L = 0 \quad \phi_R \delta_R^{(2)} \phi_R = 0$$

def.

$$\phi_L = \begin{pmatrix} x_L \\ y_L \\ z_L \end{pmatrix} \nu_L \quad \phi_R = \begin{pmatrix} x_R \\ y_R \\ z_R \end{pmatrix} \nu_R$$

$$\delta_{L,R}^{(1)} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix} \delta_{L,R} \quad \delta_{L,R}^{(2)} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \delta_{L,R}$$

$$x_L^2 + y_L^2 + z_L^2 = 3$$

$$x_R^2 + y_R^2 + z_R^2 = 3$$

$$x_L^2 + y_L^2 - 2z_L^2 = 0$$

$$x_R^2 + y_R^2 - 2z_R^2 = 0$$

$$x_L^2 - y_L^2 = 0$$

$$x_R^2 - y_R^2 = 0$$

$$x_L = y_L = z_L = 1$$

$$x_R = y_R = z_R = 1$$

$$\delta^{(i)} = \begin{pmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & -a-b \end{pmatrix}$$

$$\delta W = \frac{K_Q}{M_f^2} \left\{ A_i^Q (\bar{e} \delta_R^{(i)} \phi_R) (\phi_L \ell) \right. \\ \left. + B_i^Q (\bar{e} \phi_R) (\phi_L \delta_L^{(i)} \ell) + C_{ij}^Q (\bar{e} \delta_R^{(i)} \phi_R) (\phi_L \delta_L^{(j)} \ell) \right\} \bar{H}$$

$$\bar{U}_{FD}^T \hat{m}_\ell \bar{U}_{FD} = K_Q \left(\frac{v_L v_R}{M_f^2} \right) \langle \bar{H} \rangle \times$$

$$\begin{pmatrix} 2 C_{22}^Q \epsilon_L \epsilon_R & 2\sqrt{3} C_{21}^Q \epsilon_R \delta_L & \sqrt{6} A_2^Q \epsilon_R \\ 2\sqrt{2} C_{12}^Q \epsilon_L \delta_R & 6 C_{11}^Q \delta_L \delta_R & 3\sqrt{2} A_1^Q \delta_R \\ \sqrt{6} B_2^Q \epsilon_L & 3\sqrt{2} B_1^Q \delta_L & 3 \end{pmatrix} /_{RL}$$

μ and e get masses!

$$m_\mu / m_\tau \simeq \delta_L \delta_R \quad m_e / m_\tau \simeq \epsilon_L \epsilon_R$$

Quark Mass Matrices

$$A_i^Q \rightarrow A_i^{U,D} \quad B_i^Q \rightarrow B_i^{U,D} \quad C_{ij}^Q \rightarrow C_{ij}^{U,D}$$

$$V_{us} \simeq \frac{\epsilon_L}{\delta_L}, \quad V_{cb} \simeq \delta_L, \quad V_{ub} \simeq \epsilon_L$$

$$\delta_L \simeq \lambda^2 \quad \epsilon_L \simeq \lambda^3 \quad \delta_R \simeq 1 \quad \epsilon_R \simeq \lambda$$

Δm_{ij}^2 are related with δ_L and ϵ_L

$$\delta W = \frac{H^2}{M} \rho \left(\beta \frac{\phi_L}{M_4} \frac{\phi_L}{M_4} \right) \rho$$

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$$\hat{m}_\nu = \frac{\langle H \rangle^2}{M} \left\{ \begin{aligned} & \left(\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right) + d_{(1)} \left(\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{array} \right) \delta_L \\ & + d_{(2)} \left(\begin{array}{ccc} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{array} \right) \epsilon_L + \beta \left(\frac{v_L}{M_4} \right)^2 \left(\begin{array}{ccc} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{array} \right) \end{aligned} \right\}$$

In the case of $\beta \left(\frac{v_L}{M_4} \right)^2 \ll d_{(2)} \epsilon_L$

$$m_{\nu_3} = m_0 (1 - 2d_{(1)} \delta_L) \quad m_0 \equiv \frac{\langle H \rangle^2}{M}$$

$$m_{\nu_2, \nu_1} = m_0 (1 + d_{(1)} \delta_L \mp d_{(2)} \epsilon_L)$$

$$\Delta m_{31}^2 \approx 6 |d_{(1)} \delta_L|, \quad \Delta m_{21}^2 \approx 4 |d_{(2)} \epsilon_L|$$

$$\Delta m_{21}^2 \approx \frac{\epsilon_L}{\delta_L} \Delta m_{31}^2$$

Input: $\delta_L \approx 0.1$ $\epsilon_L \approx 10^{-3} \sim 10^{-2}$

$$\Delta m_{21}^2 \approx 10^{-5} \sim 10^{-4} \text{ eV}^2 \quad (\text{prediction}) \quad \Delta m_{31}^2 = 10^{-3} \text{ eV}^2$$

$$U_{MNS} = (A B_\rho^\dagger) = B_\rho^\dagger A^T = B_\rho^\dagger \begin{pmatrix} \boxed{\frac{1}{\sqrt{2}}} & \boxed{\frac{1}{\sqrt{2}}} & 0 \\ \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{6}} & \boxed{\frac{2}{\sqrt{6}}} \\ \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{3}} & \boxed{\frac{1}{\sqrt{3}}} \end{pmatrix}$$

$$B_\rho^\dagger \approx \begin{pmatrix} 1 & -\lambda & \lambda^3 \\ \lambda & 1 & -\lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

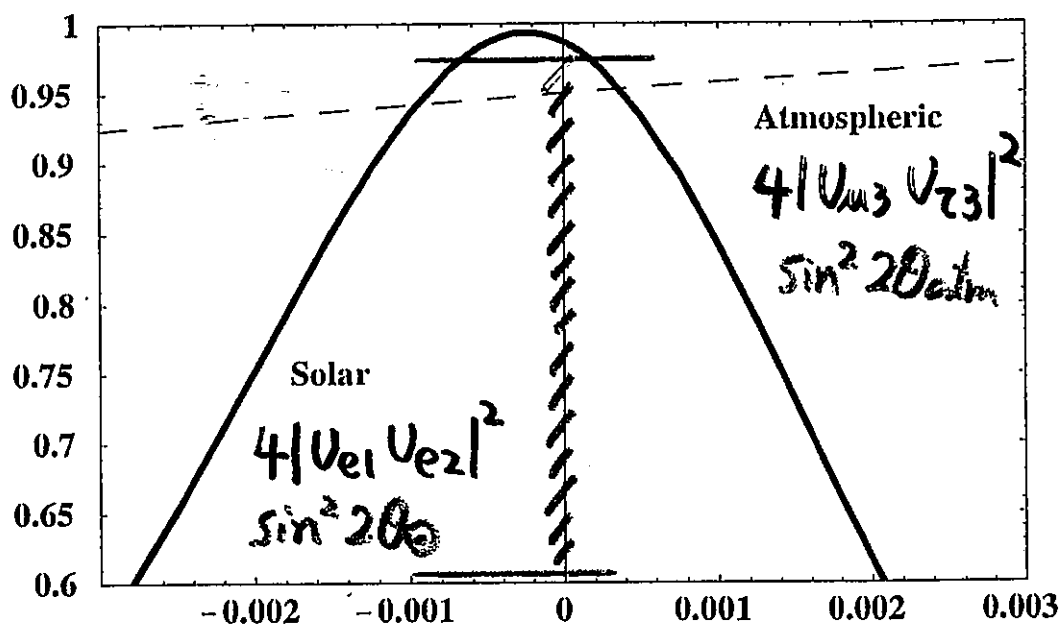
Large Mixing Angle MSW solution !!

$$m_0 = 0.1 \text{ eV} \quad \delta_L = 0.05 \quad \epsilon_L = 0.003$$

$$\Delta m_{31}^2 = 3.1 \times 10^{-3} \text{ eV}^2 \text{ (Atmospheric)}$$

$$\Delta m_{21}^2 = 1.1 \times 10^{-4} \text{ eV}^2 \text{ (Solar)}$$

Effect of $\beta \left(\frac{v_L}{M_f}\right)^2 \begin{pmatrix} | & | & | \\ | & | & | \\ | & | & | \end{pmatrix}$



$$\beta \left(\frac{v_L}{M_f}\right)^2$$

PL B483 (2000)417

hep-ph/0001306 Large Mixing Angle MSW solution

$$\left\{ \begin{array}{l} \sin^2 2\theta_{\odot} = 0.60 \sim 0.97 \quad (3\sigma) \\ \Delta m_{\odot}^2 = (1.4 \sim 18) \times 10^{-5} \text{ eV}^2 \end{array} \right.$$

Wait KamLAND

5 Bi-Maximal Mixings と その他 の $\bar{\nu}\nu$ L 19

= Non see saw = M_E : Diagonal

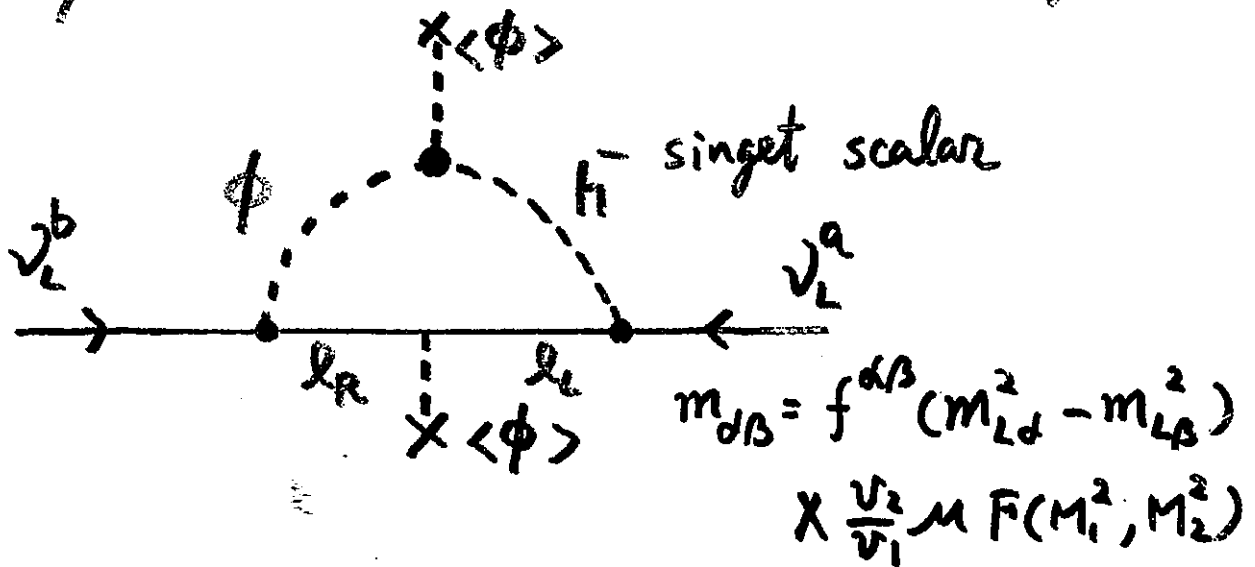
Left handed majorana masses are given

by $\nu_L^T C \langle \Delta^0 \rangle \nu_L$ $SU(2)$ triplet Higgs

$$2 \times 2 = 1, 3$$

Additional Symmetry: $L_e - L_\mu - L_\tau, \dots$

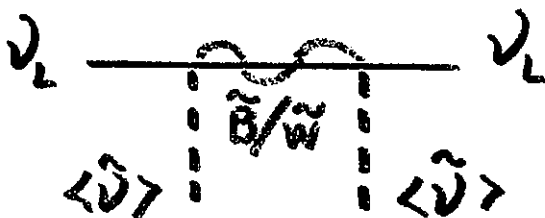
by Zee-like models $SU(2)$ singlet scalar



by R-parity and lepton-number-violation

in SUSY

$\epsilon_i L_i H$



+ loop diagrams

Typical form for M_ν

$$M_\nu = \begin{pmatrix} m_{11} & CM & SM \\ CM & m_{22} & m_{23} \\ SM & m_{23} & m_{33} \end{pmatrix}$$

$$M \gg m_{ij}, \quad S \equiv \sin\theta \quad C \equiv \cos\theta \quad \theta \sim \frac{\pi}{4}$$

\Downarrow rotation in the 2-3 plane by θ

$$M'_\nu = \begin{pmatrix} m_{11} & M & 0 \\ M & m'_{22} & m'_{23} \\ 0 & m'_{23} & m'_{33} \end{pmatrix} \quad \begin{array}{l} \text{1-2 plane} \\ \text{Large Mixing} \end{array}$$

$$m_1 \approx m_2 \gg m_3$$

$$\theta_{eu} \approx \frac{\pi}{4} \quad \theta_{\mu\tau} \approx \frac{\pi}{4}$$

$$\Delta m_{12}^2 \approx 4Mm_{ij} \quad \Delta m_{23}^2 \approx M^2 \quad M \approx 0.05 \text{ eV}$$

$$\text{LMA MSW: } m_{ij} \approx 10^{-4} \sim 10^{-3} \text{ eV}$$

$$\sin^2 2\theta_{eu} \approx 0.99$$

6 $\frac{1}{2}$ \angle \times

太陽 = エトリ) options

◦ SMA MSW many models

◦ Just - SO Nomura - Yanagida SO(10)
Albright - Barr

$S_{3L} \times S_{3R}, Z_3$

Zee-like (Radiative, R2...)

⋮

◦ LMA MSW

SO(10) ?

$S_{3L} \times S_{3R}, Z_3$

$O_{3L} \times O_{3R}$ Quark - lepton unification

$$\Delta m_{12}^2 / \Delta m_{23}^2 \sim m_s / m_b$$

$$m_1 \approx m_2 \approx m_3 \rightarrow \beta\beta_{0\nu}$$

(Non-Abelian Flavor Symmetry)

Need KamLAND !!