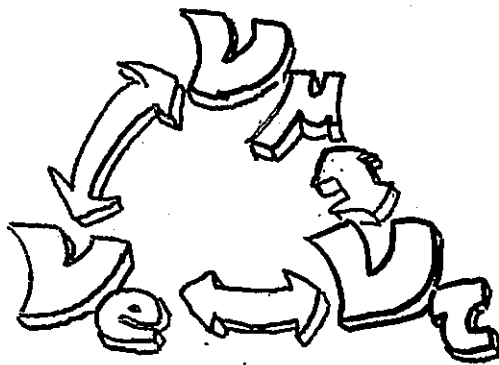


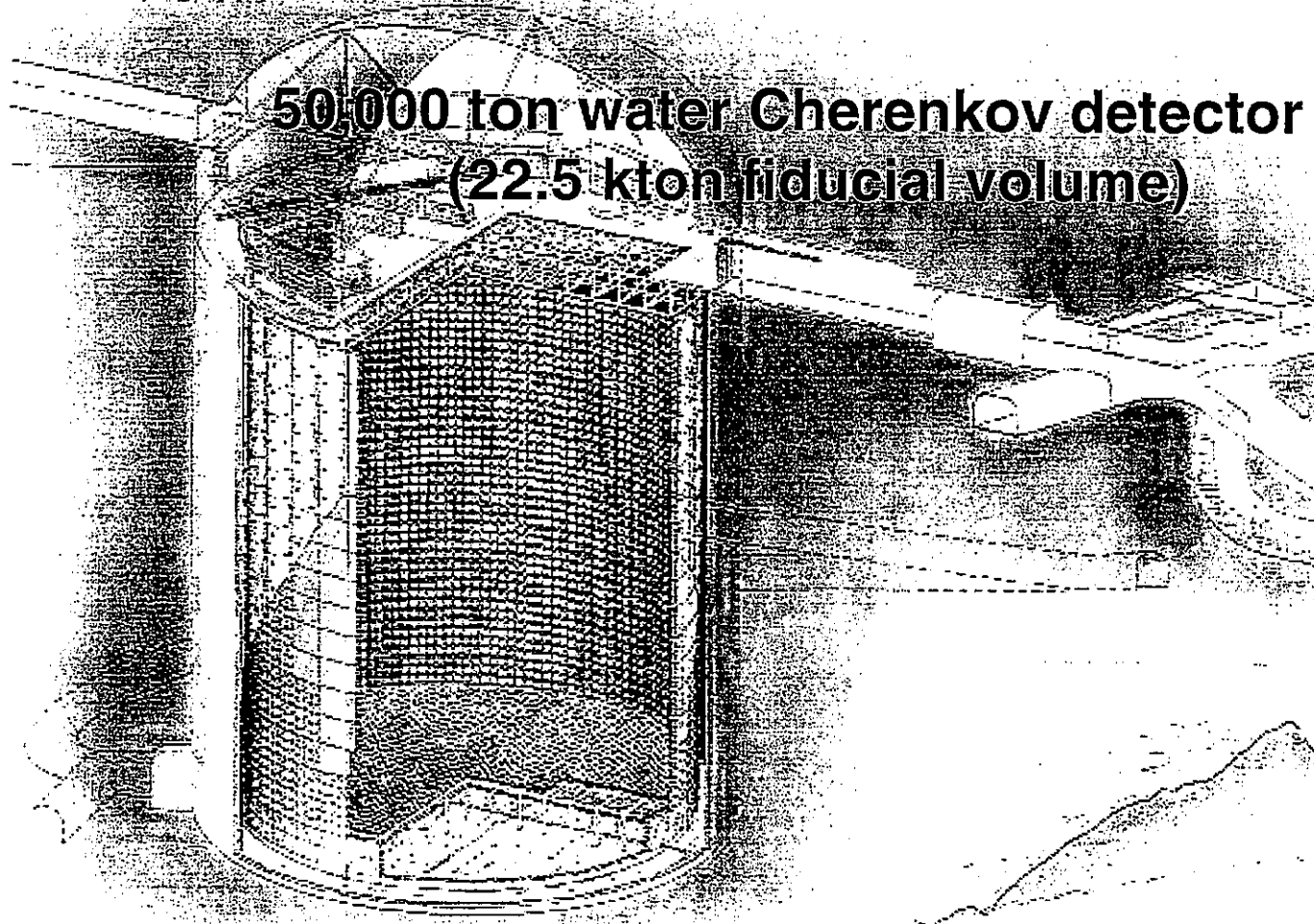
May 12, 2000 @ ICRR-Kashiwa

**Three Flavor
Oscillation Analysis
on Atmospheric
Neutrinos
@ Super-Kamiokande**



Y.OBAYASHI (ICRR, Kamioka)

Super-Kamiokade detector



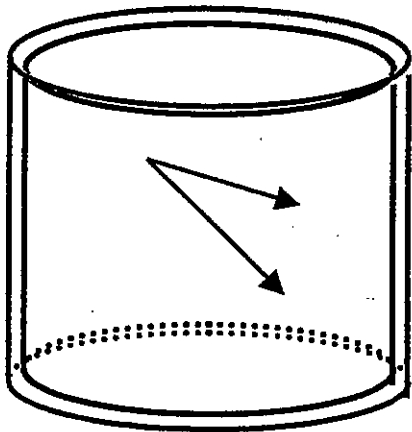
SUPERKAMIOKANDE TECHNICAL DESIGN REPORT NUMBER 071001

11,146 20-inch PMTs for inner detector

1,885 8-inch PMTs for outer detector

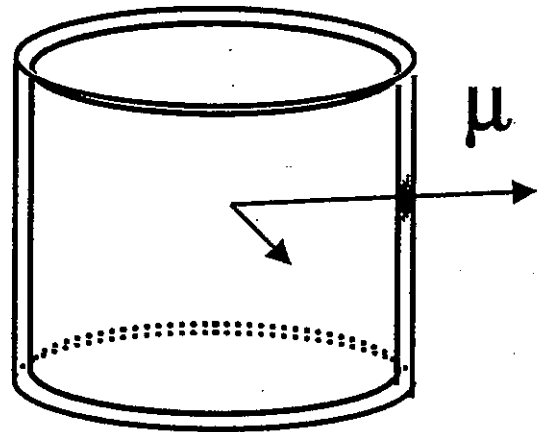
Event classification of Atm. neutrino

Fully Contained (FC)

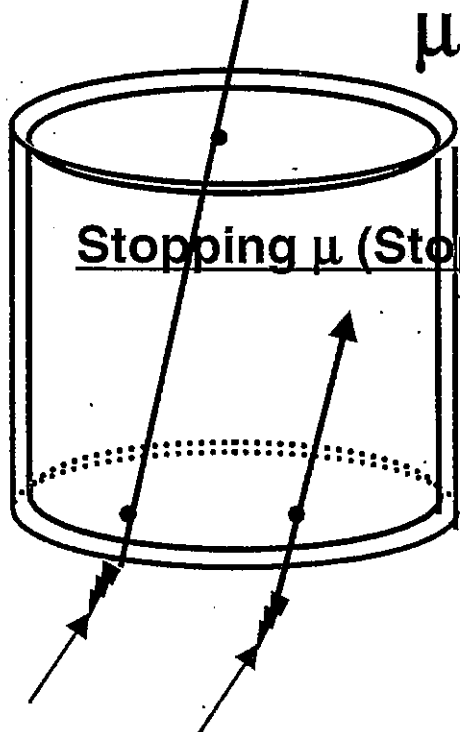


e/μ

Partially Contained (PC)

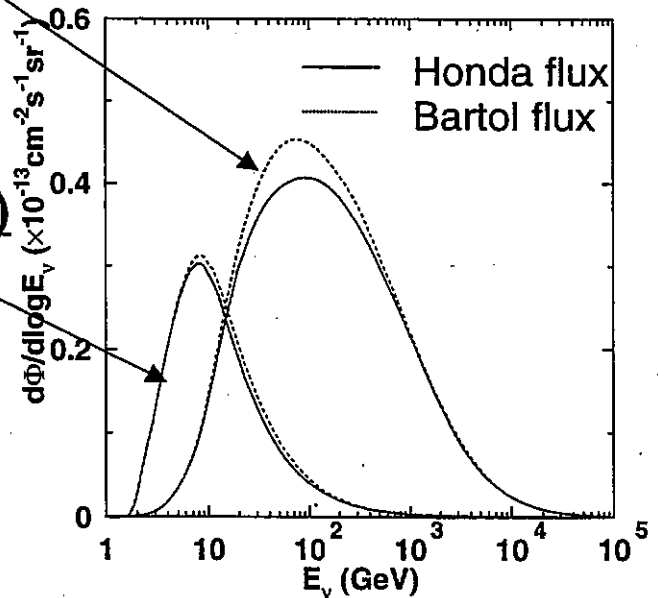


Through-going μ (Thr μ)



Stopping μ (Stop μ)

μ



Event Summary (991.6 d (61.1 kt·y))

Sub-GeV (Fully Contained)

$E_{\text{vis}} < 1.33 \text{ GeV}, P_e > 100 \text{ MeV}, P_\mu > 200 \text{ MeV}$

	Data	MC(Honda flux)
1ring e-like	2185	2081.8
μ-like	2178	3137.4
Multi ring	1637	2011.5
Total	6000	7230.7

$$\frac{(\mu/e)_{\text{Data}}}{(\mu/e)_{\text{MC}}} = 0.661 \pm 0.020 \pm 0.052$$

Multi-GeV

Fully Contained ($E_{\text{vis}} > 1.33 \text{ GeV}$)

	Data	MC(Honda flux)
1ring e-like	492	481.3
μ-like	421	640.0
Multi ring	1027	1273.8
Total	1940	2395.1

Partially Contained (assigned as μ-like)

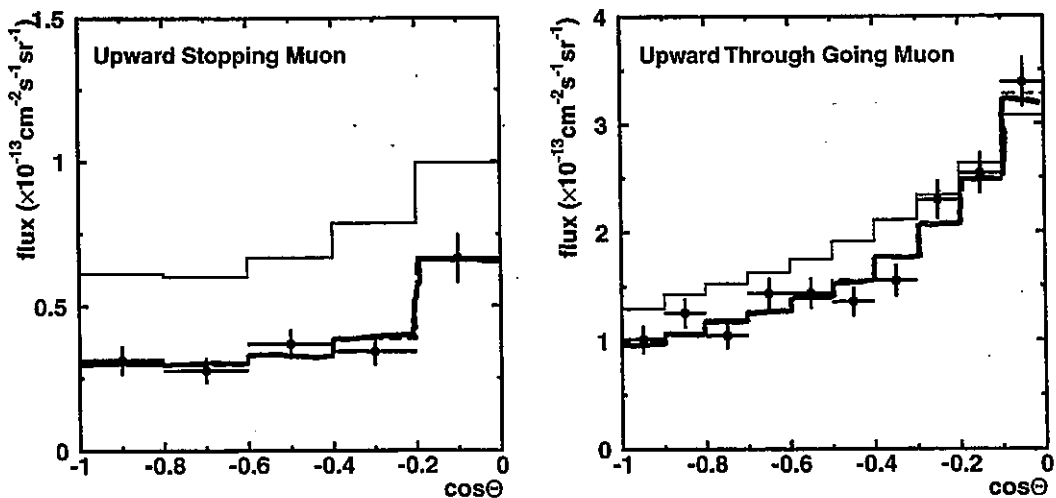
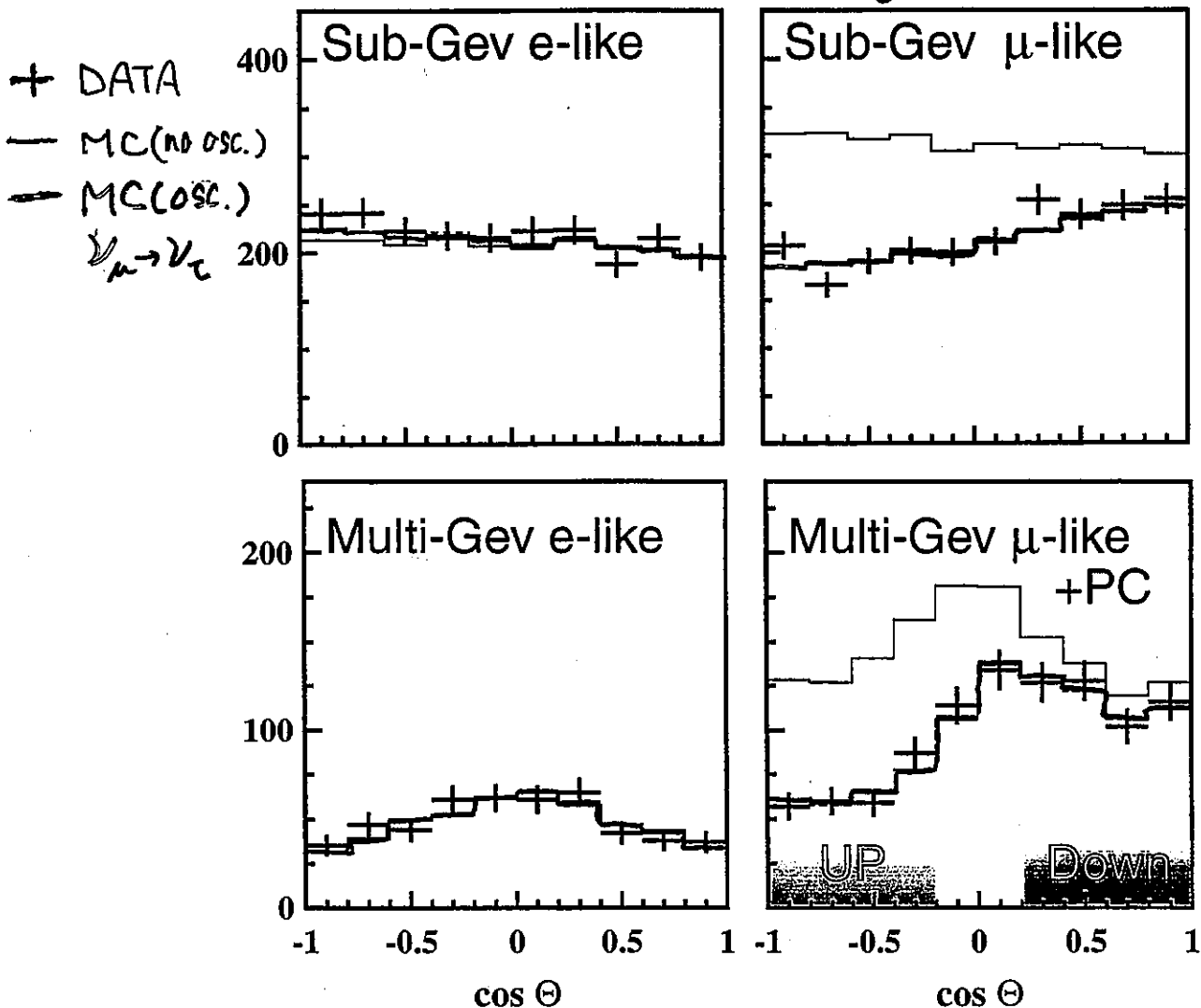
Total	563	818.9
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$$\frac{(\mu/e)_{\text{Data}}}{(\mu/e)_{\text{MC}}} = 0.660 \begin{matrix} +0.038 \\ -0.035 \end{matrix} \pm 0.078$$

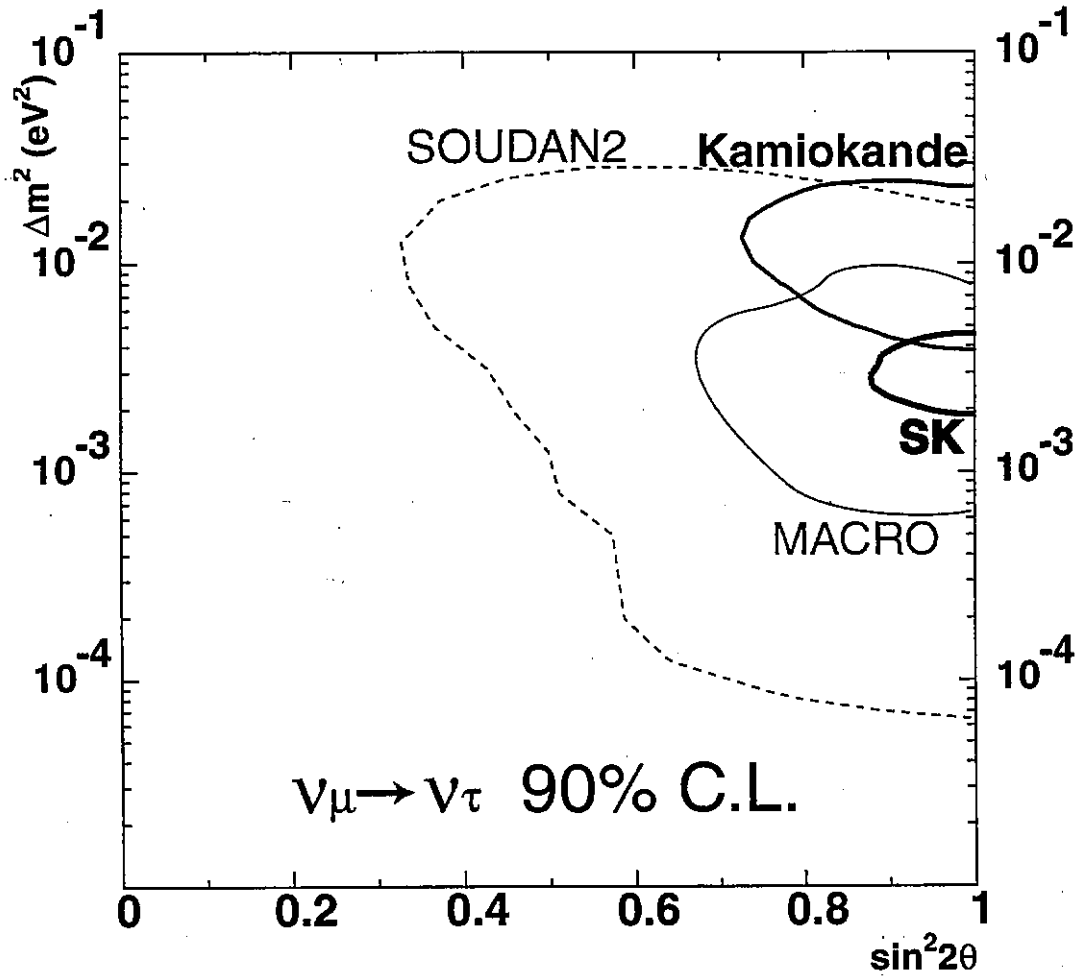
Contents

- SK990d $\nu_{\mu} \rightarrow \nu_{\tau}$ result
- θ_{13} contribution
- How can we see
Matter effect?
- Analysis result on
SK 990d data
- summary

SK 990day



$\nu_{\mu} \rightarrow \nu_{\tau}$ analysis



$$\chi^2_{\min} = 61.1/82d.o.f$$

$$@ \Delta m^2 = 2.8 \times 10^{-3} eV^2, \sin^2 2\vartheta = 1.0$$

$$2 \times 10^{-3} eV^2 < \Delta m^2 < 5 \times 10^{-3} eV^2,$$

$$0.88 < \sin^2 2\theta < 1.00$$

$$@ 90 \% \text{ C.L.}$$

$$\chi^2(\text{null osc.}) = 232.5/84d.o.f$$

3 Flavor Oscillation Analysis

- Approximation:

$$\Delta m_{23}^2 = \Delta m_{\text{atm}}^2 \approx O(10^{-3} eV^2),$$

$$\Delta m_{12}^2 = \Delta m_{\text{sol}}^2 \leq 10^{-4} eV^2 \ll \Delta m_{23}^2$$



$$P(\nu_\mu \leftrightarrow \nu_e) = \sin^2 2\theta_{13} \cdot \sin^2 \theta_{23} \cdot \sin^2(1.27 \cdot \Delta m^2 \cdot L/E)$$

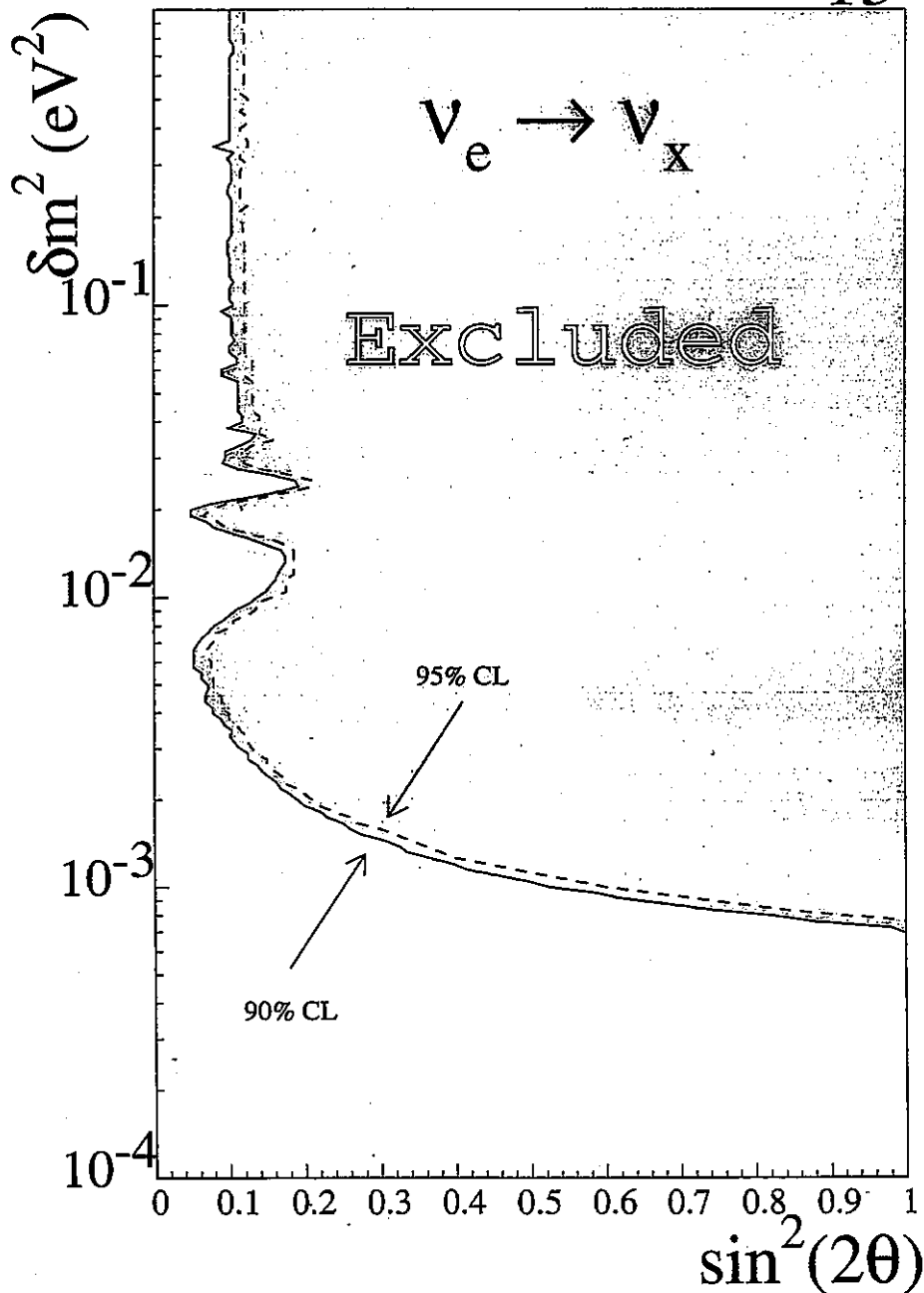
$$P(\nu_\mu \leftrightarrow \nu_\tau) = \cos^4 \theta_{13} \cdot \sin^2 2\theta_{23} \cdot \sin^2(1.27 \cdot \Delta m^2 \cdot L/E)$$

$$P(\nu_e \leftrightarrow \nu_\tau) = \sin^2 2\theta_{13} \cdot \cos^2 \theta_{23} \cdot \sin^2(1.27 \cdot \Delta m^2 \cdot L/E)$$

- P can be described only 3 parameters.

$$(\sin^2 \theta_{13}, \sin^2 \theta_{23}, \Delta m_{23}^2 = \Delta m_{13}^2)$$

Present limit on θ_{13}



$\sin^2 2\theta_{13} > 0.1$ @ $\Delta m^2 > 2 \times 10^{-3}$ is
excluded by CHOOZ

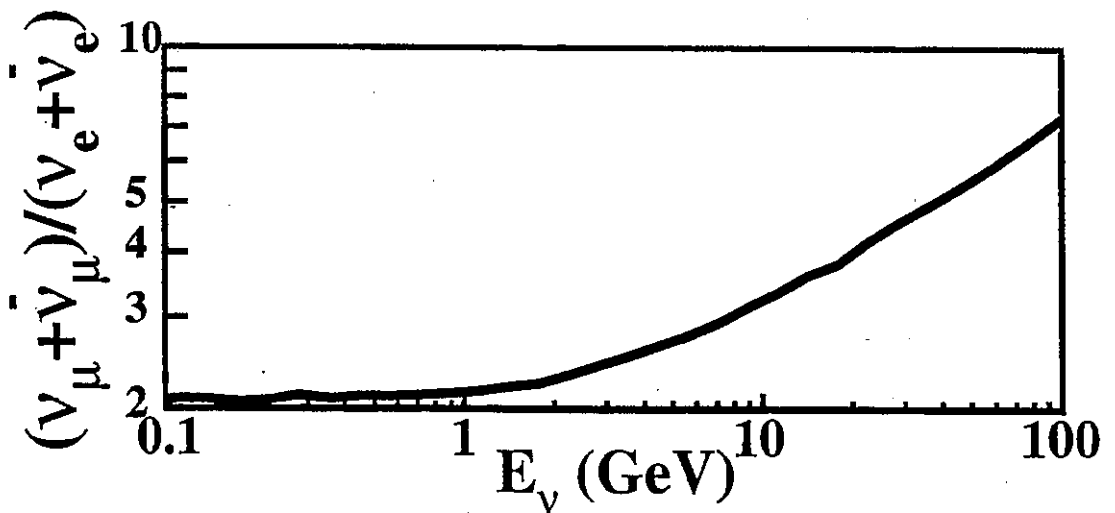
$$\sin^2 2\theta_{13} = 0.1 \rightarrow \sin^2 \theta_{13} = 0.026$$

θ_{13} contribution to atmospheric ν_e

$$\Psi = \sin^2(1.27 \Delta m^2 L / E)$$

$$\begin{aligned} \Phi(\nu_e) &= \Phi_0(\nu_e) \cdot \{1 - \sin^2(2\theta_{13})\Psi\} \\ &\quad + \Phi_0(\nu_\mu) \cdot \{\sin^2(2\theta_{13}) \cdot \sin^2 \theta_{23} \Psi\} \\ &= \Phi_0(\nu_e) \cdot \left\{ 1 + \sin^2(2\theta_{13}) \left(\underbrace{\sin^2 \theta_{23}}_{\sim 0.5} \frac{\Phi_0(\nu_\mu)}{\Phi_0(\nu_e)} - 1 \right) \cdot \Psi \right\} \\ &\hspace{15em} \downarrow \\ &\hspace{15em} \sim 2 \end{aligned}$$

Neutrino flavor ratio



$$\frac{(\nu_\mu + \bar{\nu}_\mu)}{(\nu_e + \bar{\nu}_e)} \sim 2 \text{ @ } E_\nu < 1 \text{ GeV}$$

↗ @ High E_ν

Matter Effect

In the earth:

$$\sin^2 2\theta_M = \frac{\sin^2 2\theta}{[\xi - \cos 2\theta]^2 + \sin^2 2\theta},$$
$$(\xi = 2\sqrt{2}G_F N_e \frac{E}{\Delta m^2})$$

→ resonance at

$$\frac{E(\text{GeV})}{|\Delta m^2|(\text{eV}^2)} = \frac{6.55 \times 10^3}{\frac{Z}{A} \rho(\text{g/cm}^3)} \cos 2\theta$$

$\Delta m^2 = 5 \times 10^{-3}$:

Mantle ($\rho \sim 5$)

$E \sim 12 \text{ GeV}$

Core ($\rho \sim 13$)

$E \sim 5 \text{ GeV}$

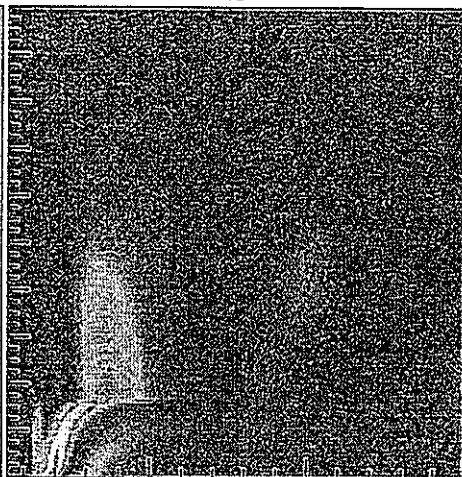
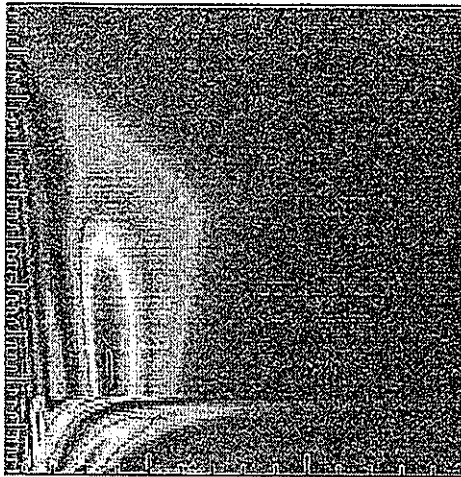
$P(\nu_e \rightarrow \nu_\mu)$

$\Delta m^2 = 0.003 \text{eV}^2$
 $\sin^2 \theta_{23} = 0.5$
 $\sin^2 \theta_{13} = 0.026$

$\Delta m^2 = 0.003 \text{eV}^2$
 $\sin^2 \theta_{23} = 0.5$
 $\sin^2 \theta_{13} = 0.005$

$\cos \Theta_\nu$

0
0.1
0.2
0.3
0.4
0.5
0.6
0.7
0.8
0.9
1



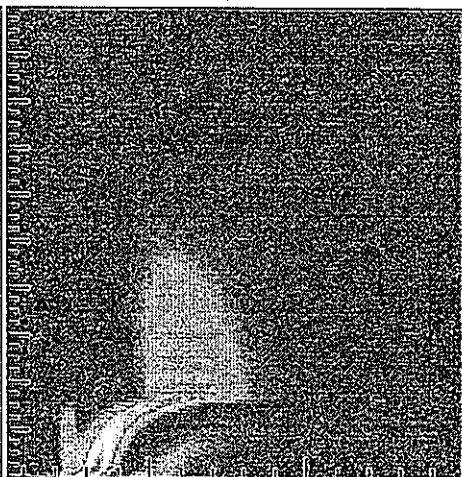
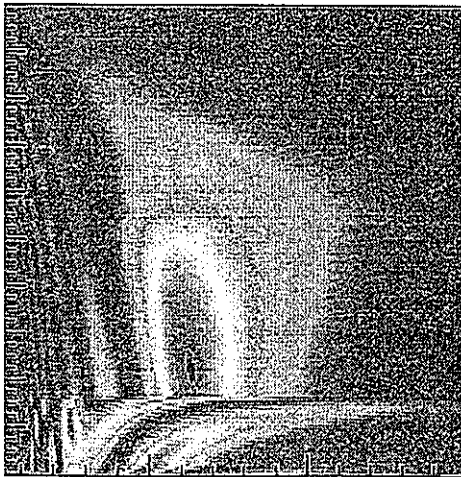
1
0.9
0.8
0.7
0.6
0.5
0.4
0.3
0.2
0.1
0

$\Delta m^2 = 0.005 \text{eV}^2$
 $\sin^2 \theta_{23} = 0.5$
 $\sin^2 \theta_{13} = 0.026$

$\Delta m^2 = 0.005 \text{eV}^2$
 $\sin^2 \theta_{23} = 0.5$
 $\sin^2 \theta_{13} = 0.005$

$\cos \Theta_\nu$

0
0.1
0.2
0.3
0.4
0.5
0.6
0.7
0.8
0.9
1



1
0.9
0.8
0.7
0.6
0.5
0.4
0.3
0.2
0.1
0

10 20 30
 E_ν (GeV)

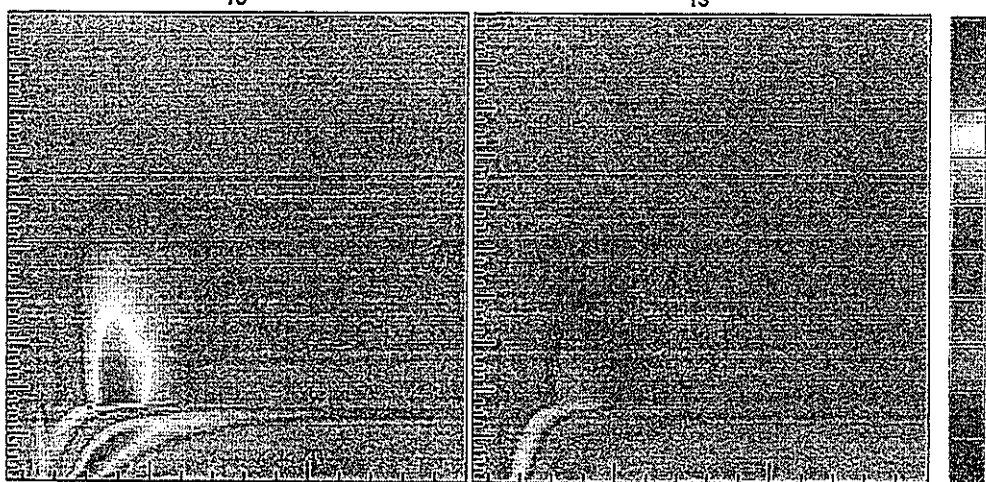
10 20 30
 E_ν (GeV)

$$(\nu_e)_{\text{osc}} / (\nu_e)_{\text{non-osc}}$$

$\Delta m^2 = 0.003 \text{eV}^2$
 $\sin^2 \theta_{23} = 0.5$
 $\sin^2 \theta_{13} = 0.026$

$\Delta m^2 = 0.003 \text{eV}^2$
 $\sin^2 \theta_{23} = 0.5$
 $\sin^2 \theta_{13} = 0.005$

$\cos \Theta_\nu$
 0
 -0.1
 -0.2
 -0.3
 -0.4
 -0.5
 -0.6
 -0.7
 -0.8
 -0.9
 -1

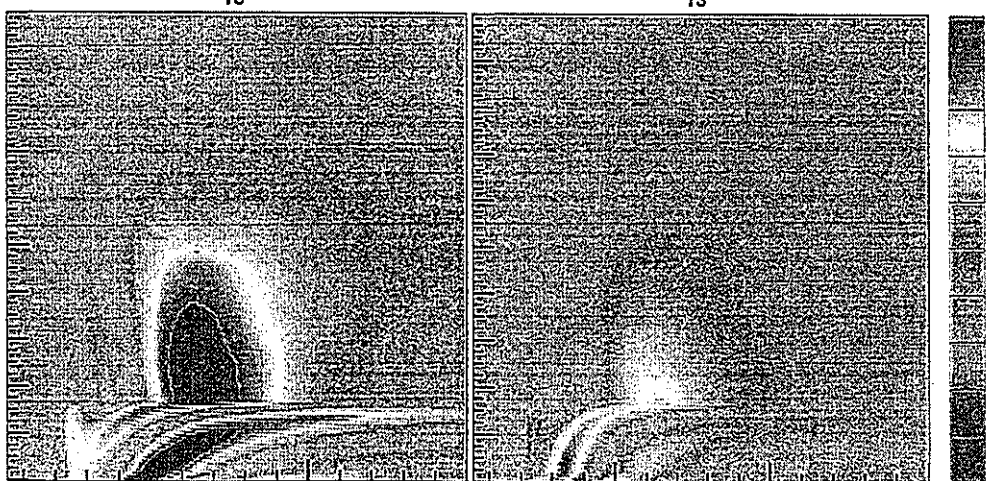


2.5
 2.25
 2
 1.75
 1.5
 1.25
 1
 0.75
 0.5
 0.25
 0

$\Delta m^2 = 0.005 \text{eV}^2$
 $\sin^2 \theta_{23} = 0.5$
 $\sin^2 \theta_{13} = 0.026$

$\Delta m^2 = 0.005 \text{eV}^2$
 $\sin^2 \theta_{23} = 0.5$
 $\sin^2 \theta_{13} = 0.005$

$\cos \Theta_\nu$
 0
 -0.1
 -0.2
 -0.3
 -0.4
 -0.5
 -0.6
 -0.7
 -0.8
 -0.9
 -1



2.5
 2.25
 2
 1.75
 1.5
 1.25
 1
 0.75
 0.5
 0.25
 0

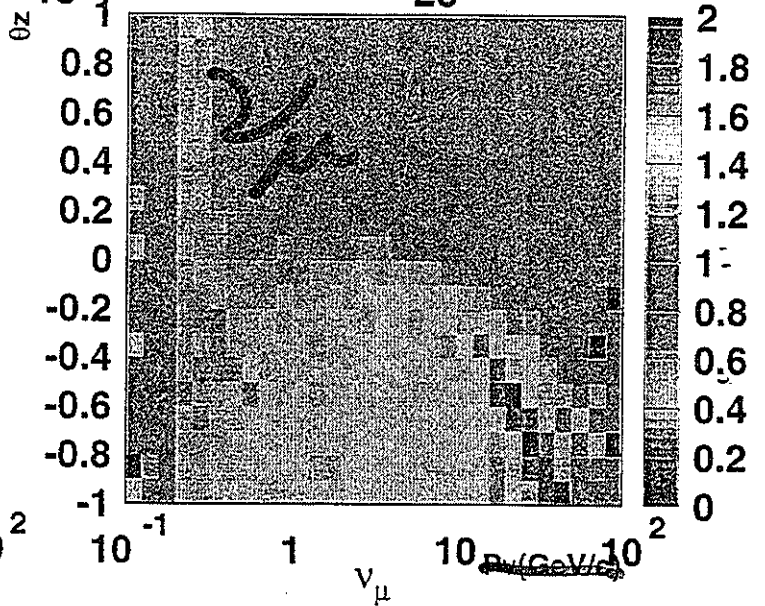
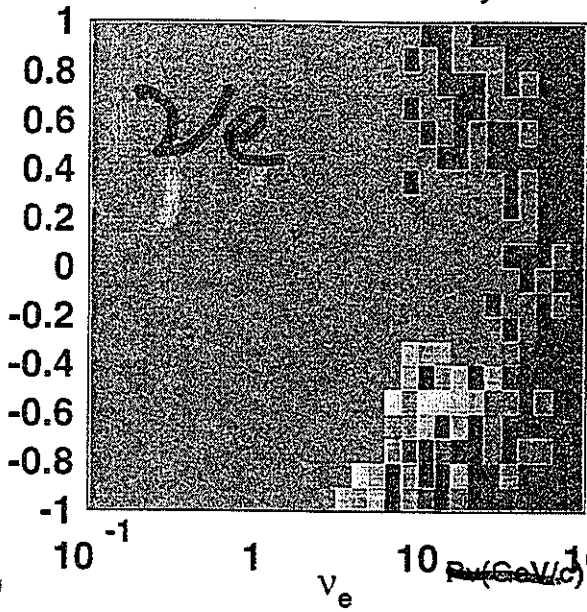
10 20 30
 E_ν (GeV)

10 20 30
 E_ν (GeV)

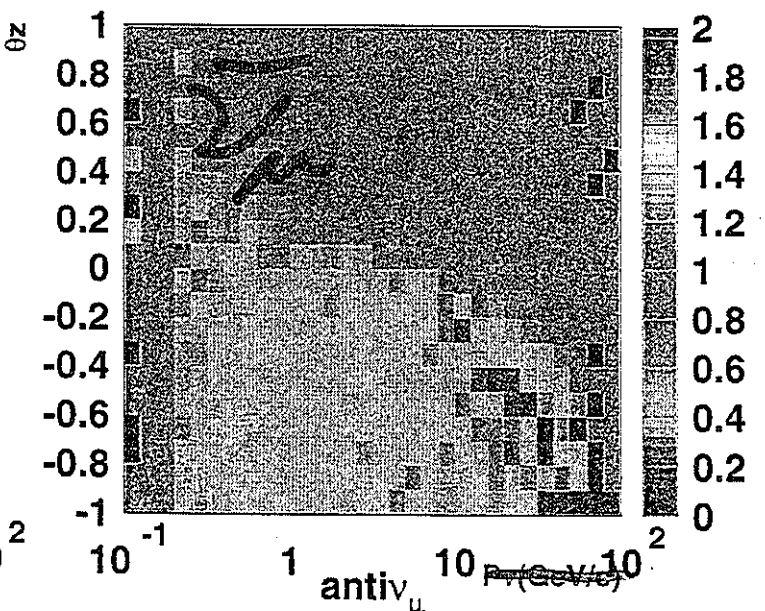
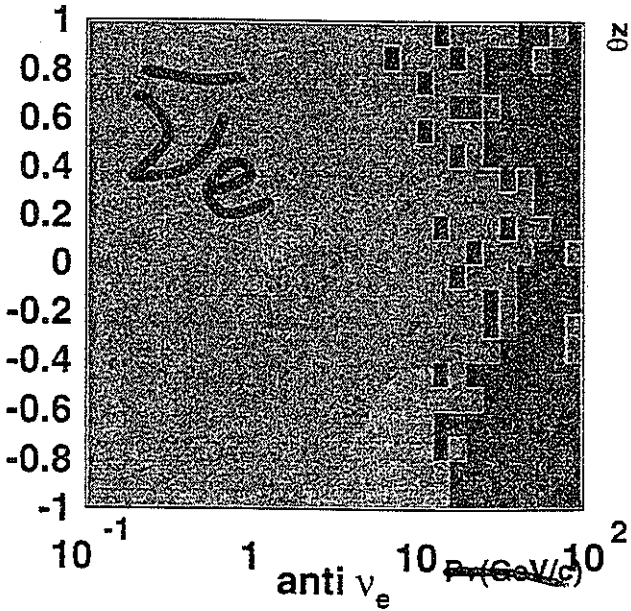
oscillated / no oscillated

measured θ_z

$\Delta m^2 = 5 \times 10^{-3} \text{ eV}^2, \sin^2 \theta_{13} = 0.026, \sin^2 \theta_{23} = 0.5$



measured θ_z



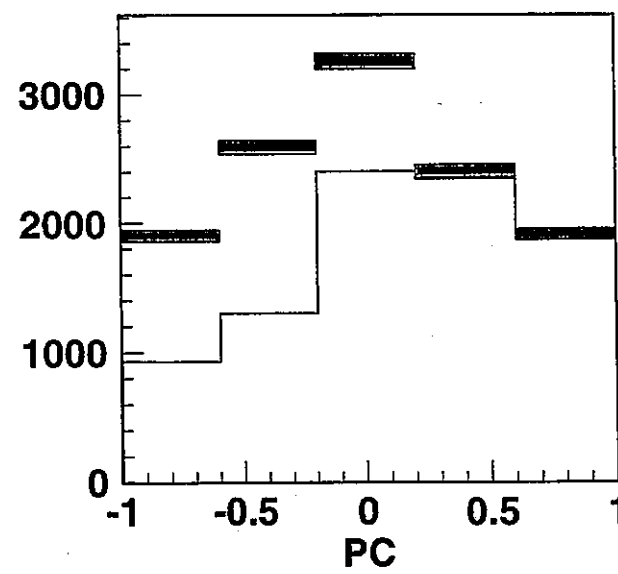
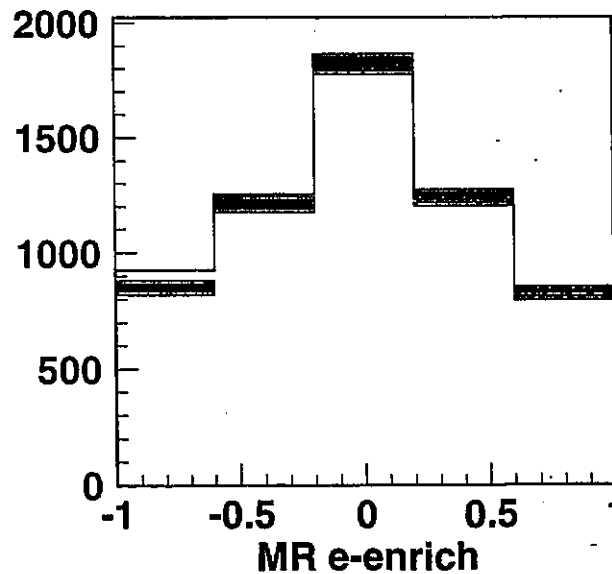
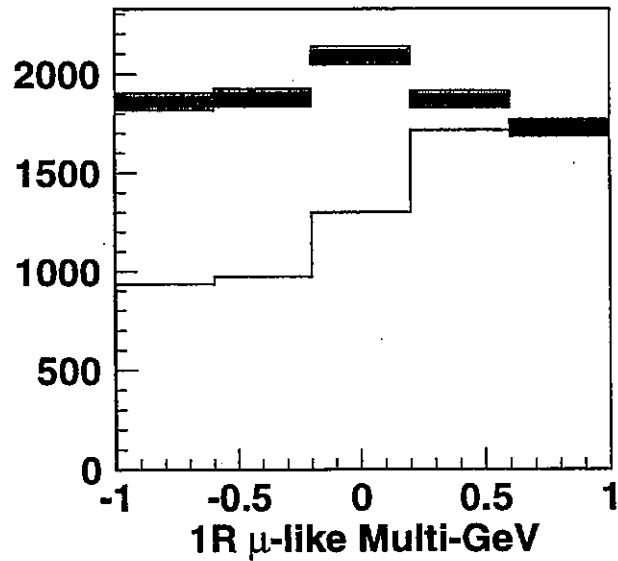
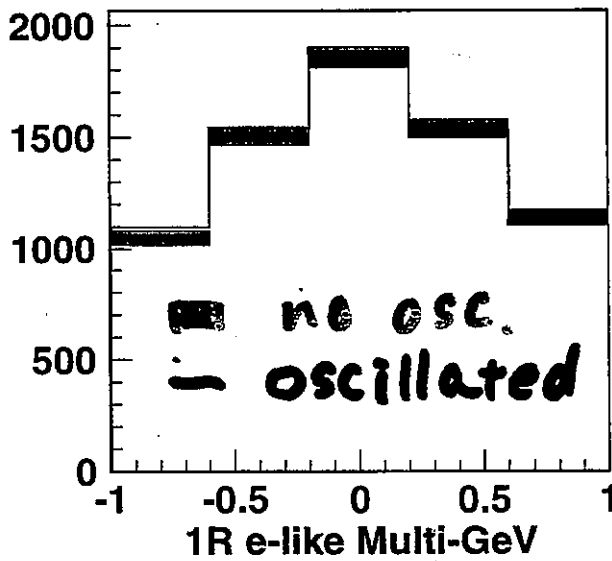
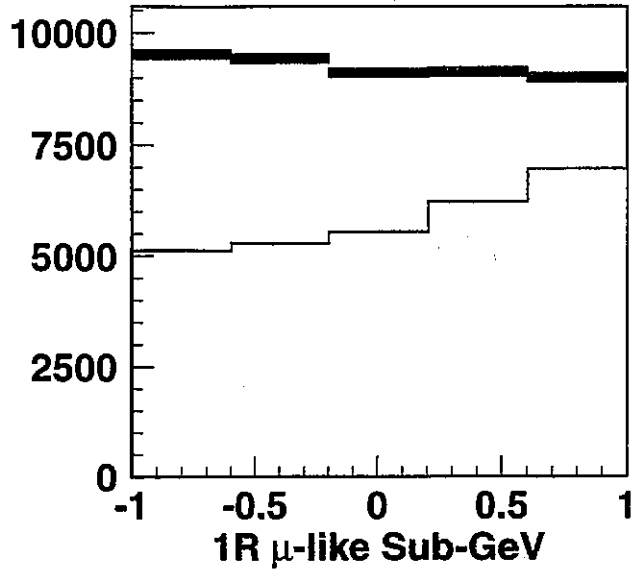
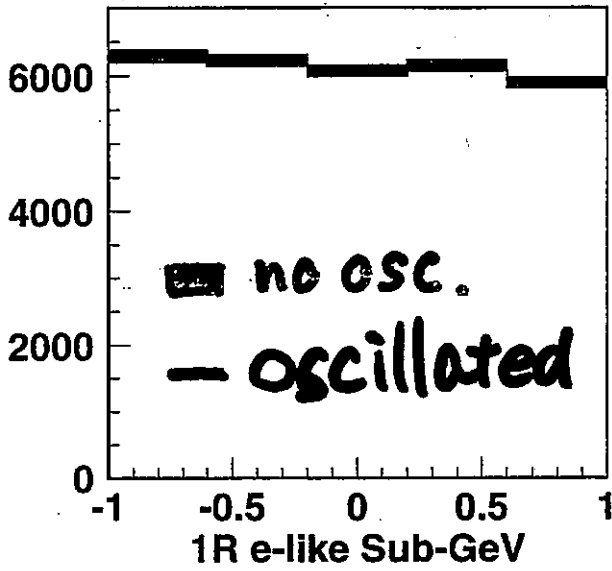
measured Plep

measured Plep

SK 40yr MC

:0/05/11 16.19

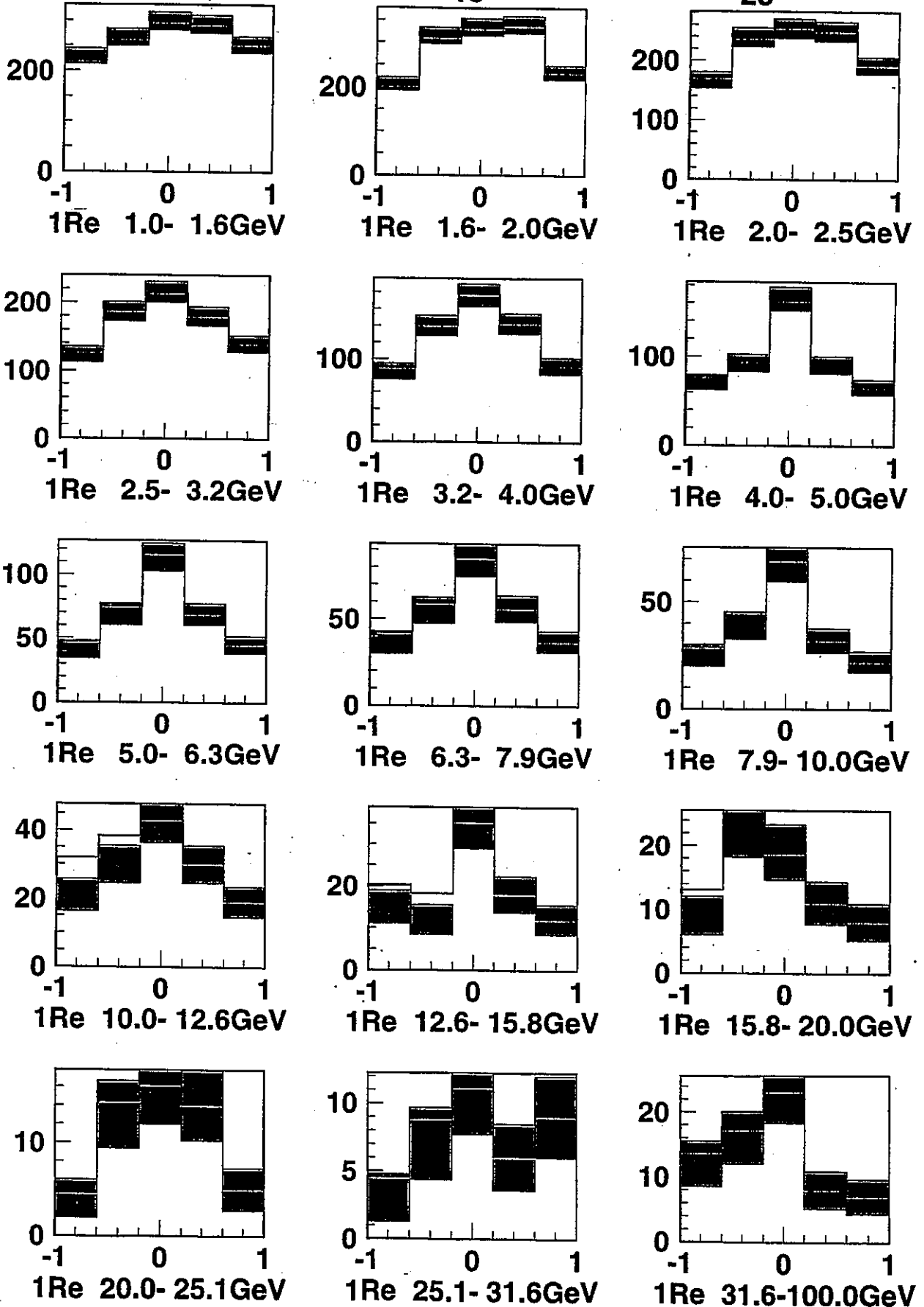
$\log(\Delta m^2) = -2.3, \sin^2 \theta_{13} = 0.026, \sin^2 \theta_{23} = 0.5$



SK 40yr MC 1ring e-like

:0/05/11 16.19

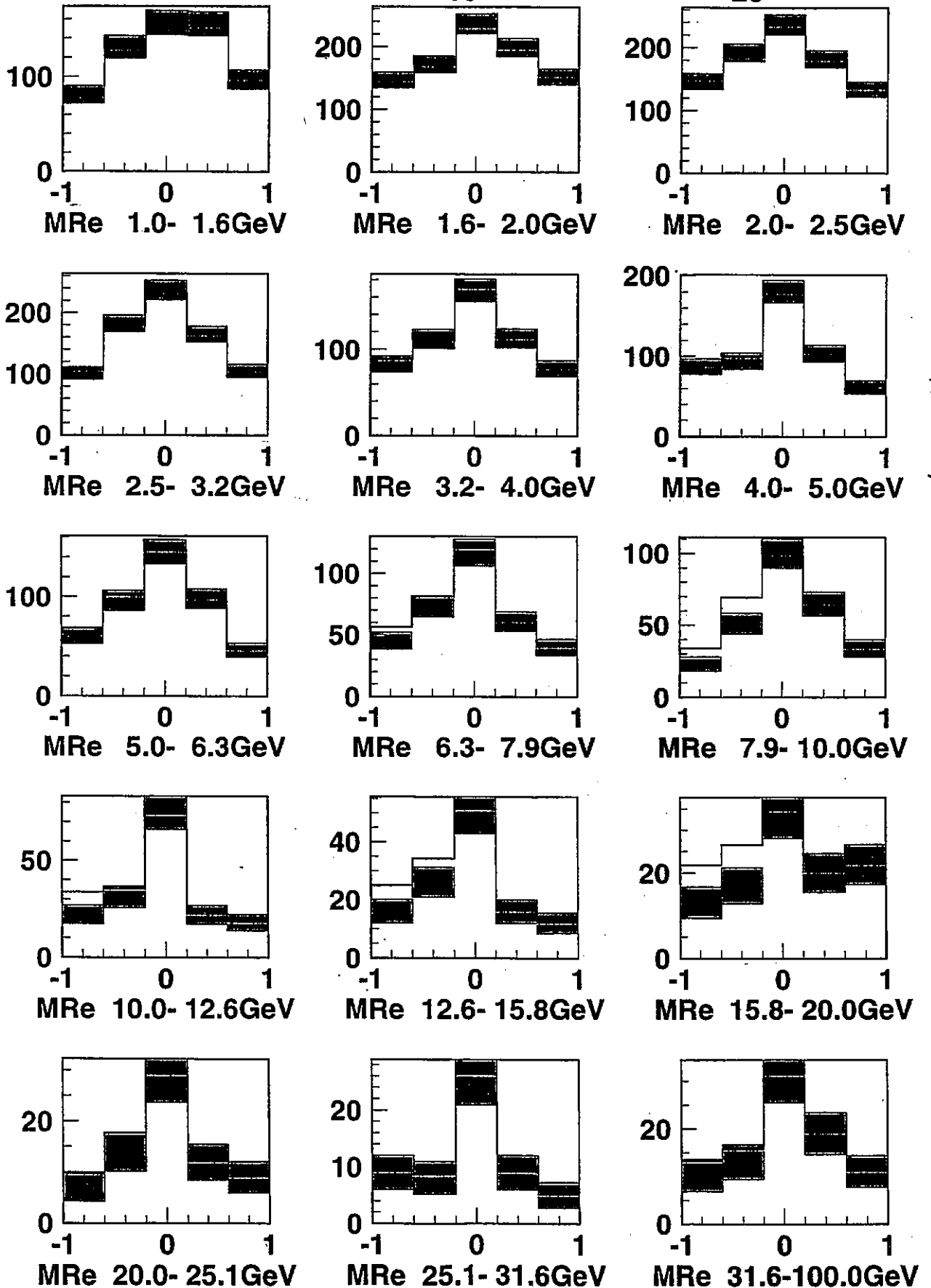
$\log(\Delta m^2) = -2.3$, $\sin^2 \theta_{13} = 0.026$, $\sin^2 \theta_{23} = 0.5$



SK 40yr MC Multi ring e-like

0/05/11 16.19

$\log(\Delta m^2) = -2.3$, $\sin^2 \theta_{13} = 0.026$, $\sin^2 \theta_{23} = 0.5$



Summary

- If $\sin^2\theta_{13} \approx 0.026$ (CHOOZ limit)
→ A excess @ $\uparrow \nu_e$
 $E_\nu \sim 10 \text{ GeV}$
($\Delta m^2 \sim 5 \times 10^{-3} \text{ eV}$)

should be observed

→ Analysis is now in progress
on SK data

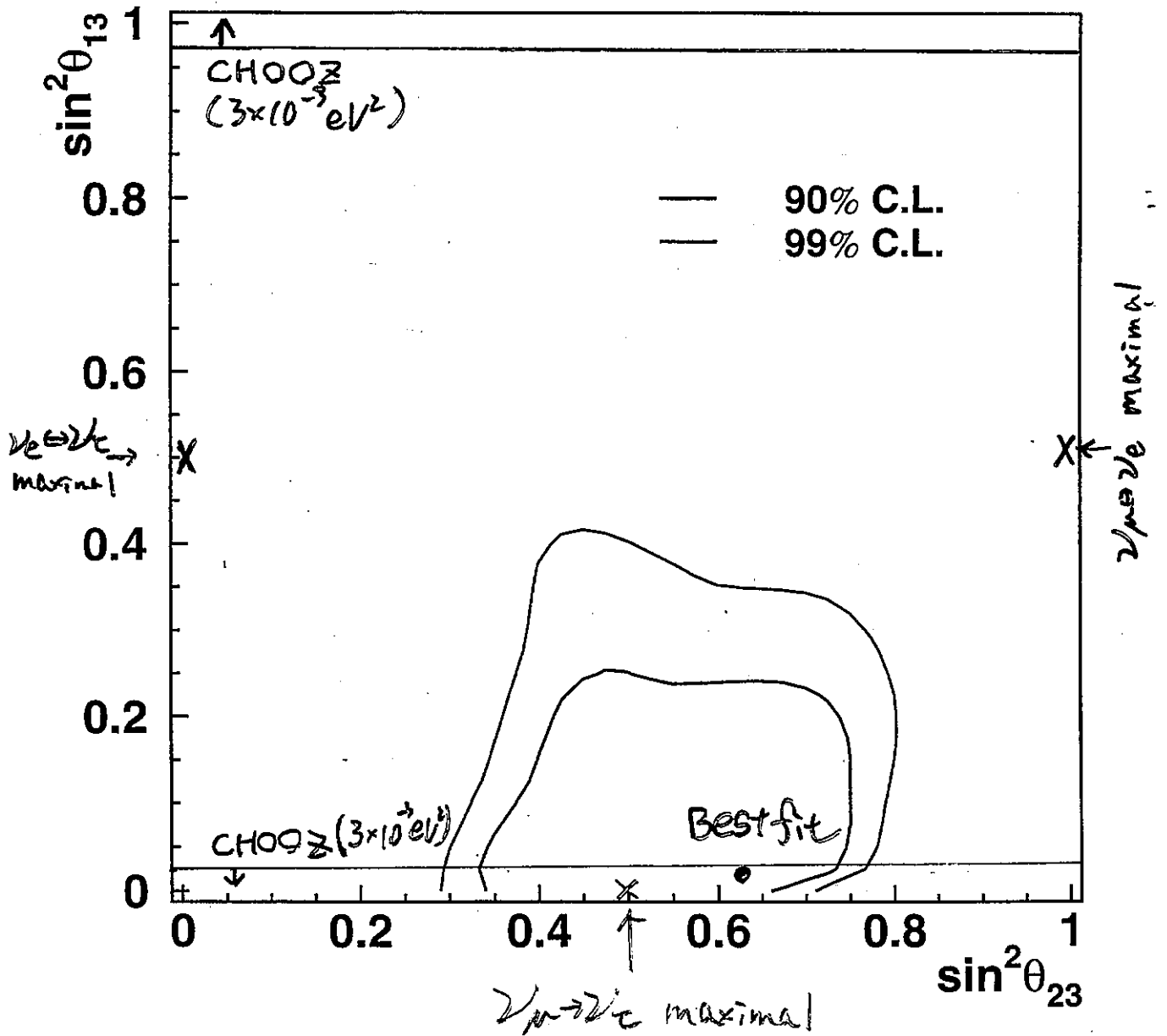
- "Standard" analysis result
on SK 990 day data:

$$\sin^2\theta_{13} < 0.25$$

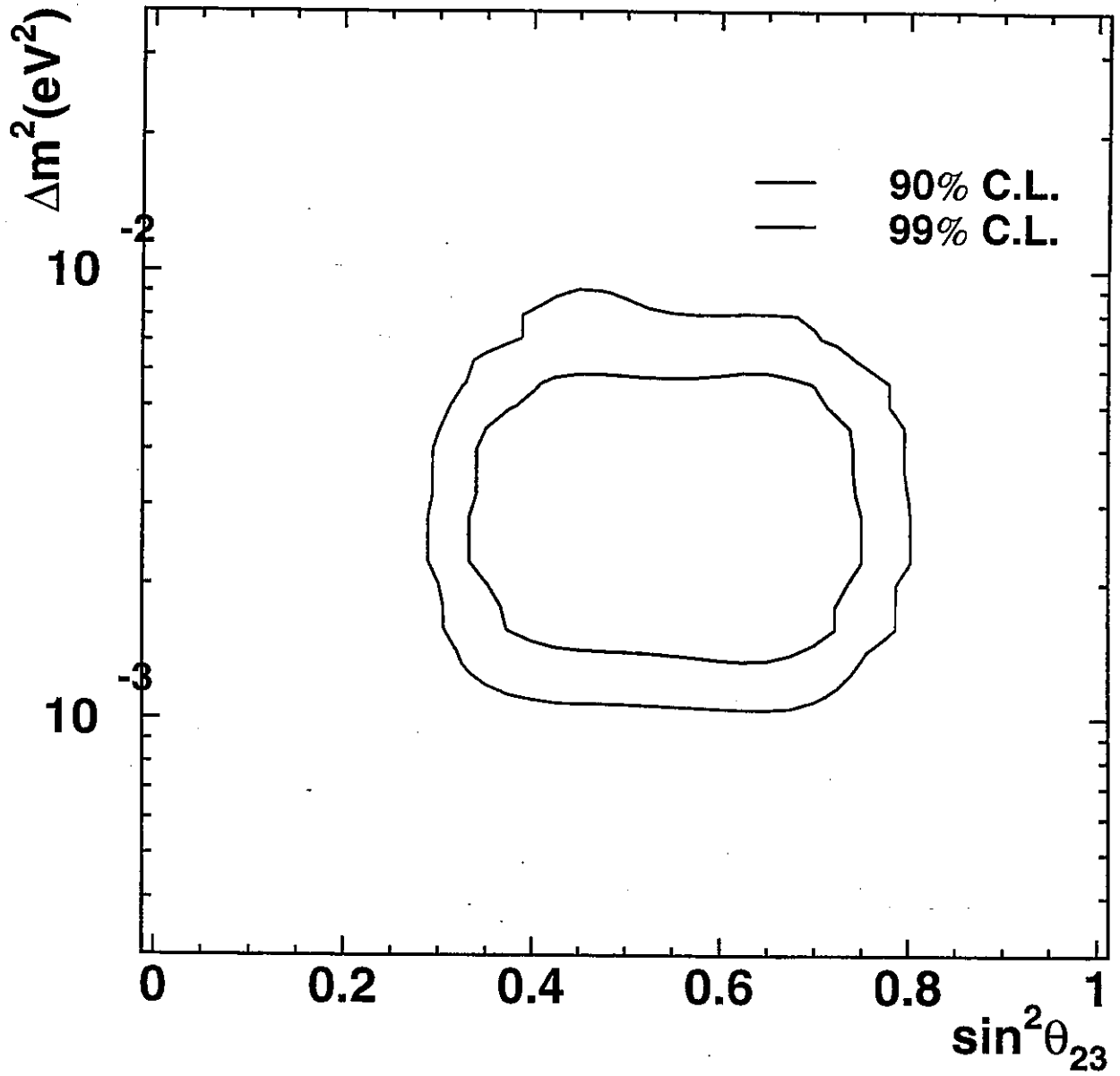
$$\text{Best fit: } \sin^2\theta_{13} = 0.025$$

$$\sin^2\theta_{23} = 0.625$$

Allowed region for
 $\sin^2\theta_{13}$, $\sin^2\theta_{23}$
 (FC+PC 990 day)



FC+PC 990 day



FC+PC 990 day

