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## The Proton Spectrum in the 0.1-100 TeV Energy Range Obtained From Direct Measurements of the All-Particle Spectrum

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### Abstract

The proton spectrum was obtained as the difference between the all-particle flux and the flux of all nuclei with  $Z \geq 2$ . The obtained spectrum has a ‘knee’ at the energy of about 1 TeV. The spectral index  $\beta_p = 2.6 - 2.7$  in the energy range  $E < 1$  TeV and  $\beta_p = 3.0 - 3.1$  in the energy range  $E \geq 1$  TeV.

The proton spectrum  $I_p(E)$  can be obtained from the obvious equality  $I_o(E) = I_p(E) + I_z(E)$ , where  $I_o$  is the all-particle spectrum, and  $I_z$  - is the spectrum of all nuclei with  $Z \geq 2$ . Multiplying all the terms of this equality by  $E^{2.6}$  and inter-substituting  $I_o$  and  $I_p$ , we obtain:

$$E^{2.6}I_p = E^{2.6}I_o - E^{2.6}I_z \quad (1)$$

In a broad range of energies  $E^{2.6}I_z = const = \Phi_z$ , therefore, expression (1) can be rewritten as  $E^{2.6}I_p = E^{2.6}I_o - \Phi_z$ . In the energy range  $E < 1$  TeV  $E^{2.6}I_o = const = 0.248 \pm 0.005m^{-2}s^{-1}sr^{-1}TeV^{1.6}$  [1] and  $\Phi_z = 0.138 \pm 0.005m^{-2}s^{-1}sr^{-1}TeV^{1.6}$ , hence,  $E^{2.6}I_p = const = 0.11 \pm 0.009m^{-2}s^{-1}sr^{-1}TeV^{1.6}$ . Thus,  $\beta_p = 2.6$ .

In the energy range  $E > 1$  TeV the all-particle spectrum index  $\beta = 2.88 \pm 0.04$ , therefore,  $\beta_p$  should be greater than 2.6. The value of  $\beta_p$  at  $E > 1TeV$  can be obtained from the all-particle spectrum characteristics, if we rewrite the proton spectrum in a somewhat simplified form: as  $I_p(E) \sim E^{-2.6}$  at  $E \leq E_c$  and as  $I_p \sim E^{-\beta_p}$  at  $E > E_c$ . For such a proton spectrum the all-particle spectrum will have the following form:  $E^{2.6}I_o(E) = BE^{-(\beta_p-2.6)} + \Phi_z$ . At  $E = E_c$  we have  $E^{2.6}I_o = \Phi_1$  and  $B = (\Phi_1 - \Phi_z)E_c^{(\beta_p-2.6)}$ . Therefore,  $E^{2.6}I_o(E) = (\Phi_1 - \Phi_z)(E/E_c)^{-(\beta_p-2.6)} + \Phi_z$ . The sum of two power-law functions  $BE^{-\gamma_1} + CE^{-\gamma_2}$  can be substituted with good accuracy by one power-law function  $DE^{-\gamma}$ , where  $\gamma = \frac{B}{C+B}\gamma_1 + \frac{C}{C+B}\gamma_2$  [2]. In our case  $\gamma_1 = \beta_p - 2.6$  and  $B = \frac{\Phi_1 - \Phi_z}{\Phi_1}$ ,  $\gamma_2 = 0$  and  $C = \Phi_z/\Phi_1$ . Therefore, the power index of the sum of the spectra will be equal to  $\frac{\Phi_1 - \Phi_z}{\Phi_1}(\beta_p - 2.6)$ . In the  $E > E_c$  energy range the spectral index of the all particle

**Table 1.**

Author and technique	$E_{min}$ , TeV	Spectral index	$N_o$
Ya.Kawamura, et al. XEC, [3]	5	$\beta_p - 1 = 1.82 \pm 0.13$	90*
N.Grigorov, calorimeter, [4]	4	$\beta_p - 1 = 2.11 \pm 0.15$	90
I.Ivanenko et al., calorimeter, [5]	5	$\beta_p = 2.85 \pm 0.14$	160*
V.Zatsepin, et al. XEC, [6]	10	$\beta_p = 3.14 \pm 0.08$	602
JACEE collaboration, XEC,[7]	6	$\beta_p = 2.80 \pm 0.04^\times$	656

<sup>×</sup> Comment: The error of 0.04 given in the JACEE paper, has no physical sense, since it is smaller than the statistical error equal to 0.07.

spectrum is equal to  $\beta$ . Therefore,  $E^{2.6}I_o(E)$  is a power-law function with the index of  $\beta - 2, 6$ . Therefore,  $\frac{\Phi_1 - \Phi_z}{\Phi_1}(\beta_p - 2.6) = (\beta - 2.6)$ . If we use the mean values from Table 2 [1] ( $\Phi_1 = 0.249 \pm 0.007$ ) and Table 1 [1] ( $\beta - 2.6) = 0.24 \pm 0.035$  and  $\Phi_z = 0.138 \pm 0.005$ , we obtain  $\beta_p - 2.6 = (0.24 \pm 0.035) \times (2.26 \pm 0.18) = 0.54 \pm 0.09$  and  $\beta_p = 3.14 \pm 0.09$  in the energy range  $E > 1$  TeV.

Therefore, the ‘step’ in the all-particle spectrum inevitably leads us to the conclusion that the proton spectrum has a ‘knee’ at energies close to 1 TeV. The shape of the proton spectrum may be obtained from the same expression (1), if we subtract from function  $\Phi(E)$ , describing the all-particle spectrum [1] the contribution of nuclei  $\Phi_z$ . In this case the proton spectrum will have the form

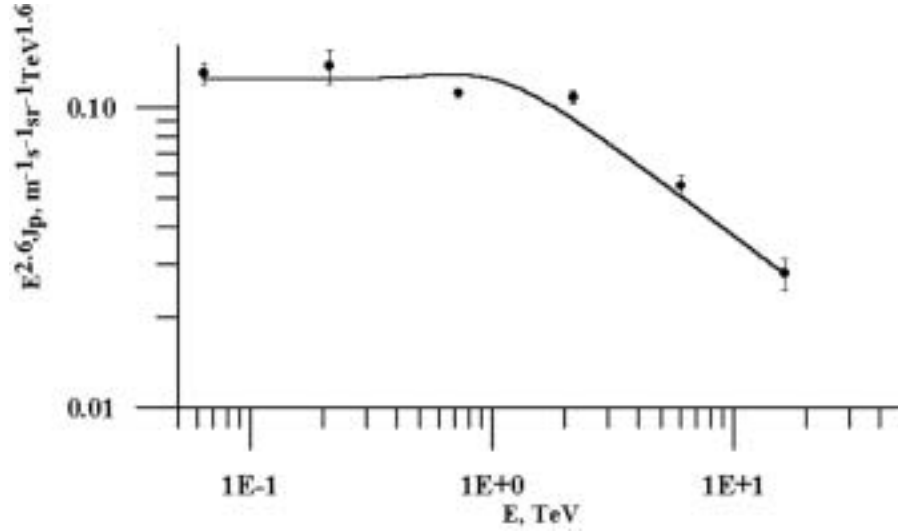
$$E^{2.6}I_p(E) = \frac{0.11}{[1 + (E/a)^3]^{0.2}} \left\{ 1 + 0.37 \frac{(E/a)^3}{1 + (E/a)^3} \right\} m^{-2} s^{-1} sr^{-1} TeV^{1.6} \quad (2)$$

It is important to stress, that the proton spectrum (2), which has a ‘knee’ at  $E = a$  was obtained from the all-particle spectrum, i.e. from experiments in which the particle backscatter from the ionization calorimeter is of absolutely no concern.

Below we will consider the results of direct measurements of protons. Table 1 shows the values of the  $\beta_p$  indices obtained in different papers. The first column contains the author and measuring technique, the second column - the minimum energy of protons in the spectrum (in TeV), the third one - the value of  $\beta_p$ , given in the paper with its error and the fourth one - the number of protons  $N_o$  used to plot the spectrum. The  $N_o$  values were given in the paper and the  $N_o^*$  values were estimated by us according to the values of the statistical errors.

The mean value  $\beta_p$  from the five measurements given in table 1 is equal to  $\langle \beta_p \rangle = 2.94 \pm 0.07$ . It is in good agreement with the value of  $\beta_p = 3.14 \pm 0.09$  for the energy range of 1 – 5 TeV (the region of the ‘step’ in the all-particle spectrum).

The XEC in [3,7] had targets. In such chambers, as it was noted in the paper of N.Konovalova [8] and in [9], the protons with energies close to the recording



**Fig. 1.** The proton spectrum measured by the SEZ-14 instrument [2]. The curve is an approximation of the difference between the all-particle spectrum and the spectrum of nuclei with  $z \geq 2$  (formula 2).

threshold, are measured with low efficiency, leading to a decrease of the value of  $\beta_p$ . Therefore, we determined  $\beta_p$  for energies  $E \geq 20$  TeV, further away from the threshold energy in spectra [6] and [7]. It turned out, that in these spectra in the indicated energy range  $\beta_p = 3.17 \pm 0.19$  and  $3.05 \pm 0.19$ . The mean value of  $\beta_p$  is equal to  $3.11 \pm 0.14$  [10].

All the three values of  $\beta_p$ : 3.14; 2.94 and 3.11 within the error bars correspond to the same spectral index, which describes the proton spectrum in the energy range from  $\sim 1$  TeV to  $\sim 40 \div 50$  TeV. The mean-weighted value of  $\beta_p$  derived from these three values is equal to  $3.02 \pm 0.05$ .

There is only one experimentally obtained proton spectrum in the  $\sim 0.1 - 10$  TeV energy range. It was obtained over 30 years ago on the ‘Proton-2,3’ satellites and is published in integral form in [11], and in differential form in [2]. We show it in Fig.1 (from [2]) together with the proton spectrum, obtained from the all-particle spectrum – equation (2) at  $a = 0.8$  TeV. It can be seen from Fig.1 that the experimental spectrum of protons coincides with the spectrum, obtained from the all-particle spectrum, and the latter, as it was shown above, agrees with direct observations in the  $\sim 5 - 40$  TeV energy range.

Hence, it can be asserted, that all direct measurements lead to the same conclusion: the proton spectrum has a ‘kink’ at energies close to 1 TeV. Before the ‘kink’ the spectral index  $\beta_p = 2.6$  (maybe 2.7) and after the ‘kink’ it is about 0.5 – 0.6 greater, i.e. 3.0-3.1.

To this conclusion it should be added, that all indirect measurements of

secondary high-energy particles in the Earth's atmosphere (hadrons, muons, and  $\gamma$ -quants) lead to the conclusion, that in the TeV region  $\beta_p \cong 3.0$  [2].

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